Accurate Isolation Networks in Quadrature Couplers and Power Dividers

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Abstract—When quadrature couplers and power dividers are implemented in integrated circuits, accurate isolation networks cannot be realized due to the nonideal resistors and the process variations. We present an isolation network design technique which cancels the resistor parasitic effects and also increases the tolerance to variations in the resistance values. A Lange coupler and a power divider are designed at Ka-band using the proposed accurate and process-tolerant isolation networks. The improvement is analytically shown and empirically verified with our in-house GaN-based microstrip MMIC process. For the coupler, the measured return losses and isolation are better than 20 dB from DC to 40 GHz. The power divider achieves 20 dB return losses and isolation in a fractional bandwidth of 50%. Both devices maintain 20 dB performance even when the variation in sheet resistance is as high as 30%.

Index Terms—Accurate, parasitic effect, wideband, quadrature coupler, power divider, isolation, sheet resistance, process-temperature variation, tolerance, integrated circuit.

I. INTRODUCTION

Quadrature couplers and power dividers are widely used for splitting and combining RF power at the input and output of balanced amplifiers [1]. Such configurations require the isolation ports of the quadrature couplers to be terminated with 50 Ω resistors. Also, power dividers use resistors in their isolation networks.

Overall circuit performance deteriorates when return loss and isolation parameters of the splitting structure degrades. Therefore, isolation networks of the couplers and dividers must be accurate and robust to variations in process and temperature. The accuracy is vital especially for millimeter-wave integrated circuits since the resistor parasitic effects become dominant at high frequencies and post-fabrication tuning is quite difficult [2]. In order to reduce the resistor parasitic effects, isolation networks without direct ground connections are used [3] and compensation elements are also added for better matching [4]. However, such techniques are inadequate, as they are tied to accurate resistor models and do not provide tolerance to variations in the resistance values.

Optimizing the fabrication process [5] is always helpful, yet it is a costly investment and perfection is never reached, therefore, an effort on the design part is unavoidable. Use of resistors can be completely abandoned [6], but the resulting bandwidth is narrow. In this brief, we analyze the effect of non-ideal resistors in couplers and dividers, and propose accurate isolation networks which cancel the resistor parasitic effects and are also tolerant to systematic errors in the resistance values.

More recently, frequency tunable quadrature couplers [7] and power dividers [8] are presented at relatively low frequencies where the resistor parasitic effects are negligible. Our proposed isolation networks can also be used in such circuits to mitigate the performance degradation at higher frequencies as well as providing tolerance to sheet resistance variation.

II. ANALYSIS AND DESIGN

A. Nonideal Resistors in Integrated Circuits

Lumped element resistors are used at the isolation port of quadrature couplers and at the isolation network of power dividers. These resistors are typically realized by thin-film technology in monolithic microwave integrated circuits (MMIC). Sheet resistance of the film is a function of the resistive material and its thickness. However, due to the reproducibility limitations in the manufacturing process, the sheet resistance is not a constant and the designer needs to account for certain variances. In our analysis, we use \( \rho \) to denote the normalized sheet resistance which is ideally equal to 1.

A simple high frequency model for a thin-film resistor is shown in Fig. 1. Here, \( L_i \) is the inductance due to the finite length of the resistor and \( C_i \) is the capacitance due to the finite distance from the resistor to the dielectric substrate. Both parameters are a function of the resistor geometry. The intrinsic resistance \( R_i \) is scaled by \( \rho \), and we assume resistors in close proximity are scaled by the same factor, since they undergo the same manufacturing process.
represented by an S-parameter matrix $S = [S_{ij}]$, where $i, j \in \{1, 2, 3, 4\}$. We consider the first port as the input port, the third port as the output port with 90° phase difference, and the fourth port as the isolation port. The symmetrical S-parameter matrix of a quadrature coupler is given as

$$[S] = \begin{bmatrix} \Gamma_0 & F_c & F_d & I_0 \\ F_c & \Gamma_0 & I_0 & F_d \\ F_d & I_0 & \Gamma_0 & F_c \\ I_0 & F_d & F_c & \Gamma_0 \end{bmatrix}$$  \tag{1}$$

When the isolation port of a quadrature coupler is terminated with an imperfect load with a reflection coefficient of $\Gamma_L$, the S-parameters of the resulting three-port network $\mathcal{S} = [\mathcal{S}_{ij} ]$ are found using Mason’s rule [9] approximately as

$$|\mathcal{S}_{ij}| = |S_{ij} + S_{i0} S_{j0} \Gamma_L| \approx |S_{ij} + S_{i0} S_{j0} \Gamma_L| \tag{2}$$

when the reflection coefficient of the coupler and the reflection at the isolation port are small with $|\Gamma_0 \Gamma_L^2| \ll 1$.

Input reflection and transmission coefficients of the three-port network are barely affected by the accuracy of the coupler termination, as $|S_{i0}| \ll 1$.

$$|\mathcal{S}_{11}| \approx |\Gamma_0 + F_d^2 \Gamma_L| \approx |S_{11}| \tag{3}$$

$$|\mathcal{S}_{21}| \approx |F_c + F_d I_0 \Gamma_L| \approx |S_{21}| \tag{4}$$

$$|\mathcal{S}_{31}| \approx |F_d + F_c I_0 \Gamma_L| \approx |S_{31}| \tag{5}$$

On the other hand, accuracy of the coupler termination is critical for the isolation and output reflection coefficients, since $|F_d| \approx 1/\sqrt{2}$ and $|F_c| \approx 1/\sqrt{2}$ and we have

$$|\mathcal{S}_{22}| \approx |\Gamma_0 + F_d^2 \Gamma_L| \tag{6}$$

$$|\mathcal{S}_{33}| \approx |\Gamma_0 + F_c^2 \Gamma_L| \tag{7}$$

$$|\mathcal{S}_{33}| \approx |I_0 + F_c F_d \Gamma_L| \tag{8}$$

When the isolation port of a coupler is terminated with a nonideal shunt resistor with a normalized impedance of $Z_R = \rho + jX_R$, where $X_R$ is the normalized parasitic reactance, the load reflection coefficient $\Gamma_L^b$ is given by

$$|\Gamma_L^b| = \frac{Z_R - 1}{Z_R + 1}.$$

C. Termination Network Design for Quadrature Couplers

We use an accurate and process-tolerant resistive load [10] at the isolation port of a quadrature coupler to cancel out the resistor parasitic effects and increase the tolerance to sheet resistance variance. In this way, isolation and output return losses are improved allowing a higher operating frequency.

Our proposed quadrature coupler shown in Fig. 2 is terminated by two shunt resistors separated by a quarter-wave length line. When the resistors are placed closely in the circuit layout, they have the same parasitic effects and normalized sheet resistances. The quarter-wave length line inverts the impedance of the second resistor so that the nonideal effects of the resistors cancel each other. We assume that the deviations in the substrate parameters and the physical line dimensions are negligible [11]. Nevertheless, circuit simulations are repeated with reasonable asymmetry between the resistors and variations in the line impedances, and their effect on our termination network response is limited. Therefore, we rule out such secondary effects and focus on the variations in resistors.

Although resistor values and line impedance can be optimized for the bandwidth and tolerance requirements, we set the resistor values to 2$Z_0$ and the line impedance to 2$Z_0$, for simplicity. Then, the load reflection coefficient $\Gamma_L^b$ becomes

$$|\Gamma_L^b| = \frac{T(2Z_0 - 1) - j(2Z_0 - Z_R)}{T(2Z_0 + 1) + j2Z_0 - jZ_R} \tag{10}$$

where $T = \tan(\pi f/2)$ with $f = f_0$. At the center frequency $f_0$, when $T \to \infty$, the proposed termination network achieves twice the return loss (in dB-scale) of a single resistor as

$$\lim_{T \to \infty} \frac{|\Gamma_L^b|}{|\Gamma_L^0|} = \lim_{T \to \infty} \frac{T(Z_R - 1) + j2Z_0}{T(Z_R + 1) + j2Z_0} = |\Gamma_L^0|.$$

regardless of the parasitic effects and the fabrication variances. For a coupler with perfect matching $|\Gamma_0| = 0$, any improvement in the termination return loss directly translates as an improvement in the coupler isolation and output return losses as implied by equations (6)–(8).

Usually, quadrature couplers are formed using coupled lines [12] or branch-line coupler based structures [13]. The Lange coupler [14] is also a type of quadrature coupler which employs a multiplicity of interdigitated lines that are connected using crossovers to achieve tight coupling in a wide band. Since Lange couplers have compact size and their crossovers can be easily implement in our MMICs, we demonstrate our termination network with a Lange coupler design.

Our Lange coupler design attempt at $Ka$-band, where $X_R$ can be as high as 0.4, using the conventional single resistor termination has an output return loss of only 16 dB even at the center frequency. However, with the proposed termination, the coupler provides output return losses better than 25 dB with higher tolerance to variations in the process and temperature.
D. Isolation Network Design for Power Dividers

The Wilkinson power divider [15] and the Gysel power divider [16] are the two most preferred power dividing structures. Both dividers are easily realizable on a planar circuit and ideally provide low insertion loss, matched conditions at all ports, and high isolation between the output ports. Although the Wilkinson power divider has more bandwidth and occupies less area, the Gysel power divider provides higher power handling capability. However, both dividers suffer from resistor parasitic effects and sheet resistance variance.

To obtain the accuracy and process-tolerance as in the quadrature coupler, we combine the isolation networks of the Wilkinson and Gysel power dividers as shown in Fig. 3. Guan et al. [17] analyzed this structure for increasing the bandwidth and power handling capability. However, a design strategy to cancel resistor parasitic effects and increase tolerance to sheet resistance variance has not been demonstrated before.

We use even-odd mode analysis [18] to calculate the even-mode reflection coefficient \( \Gamma_o^W \) and the odd-mode reflection coefficient \( \Gamma_o^O \) shown in Fig. 4.

In the even-mode, Gysel-part of the circuit becomes negligible in a wide band, because the isolation resistor \( R_4 \) is shorted by \( Z_3 \), and the short circuit is transformed into an open circuit by \( Z_3 \). With no resistor parasitic effects, the Wilkinson divider, the Gysel divider, and the proposed divider simplify to quite similar circuits, and require \( Z_3 = \sqrt{2}Z_0 \) for perfect matching. As the parasitic capacitance \( C_3 \) of \( R_3 \) increases, the electrical length of \( Z_3 \) can be slightly increased to counterbalance its effect. Also, since the resistors are shorted in a wide band, the even-mode circuits are safe against variations in \( \rho \).

In the odd-mode, \( Z_3 \) separates the two impedances \( jZ_2T/\sqrt{R_3} \) and \( jZ_4T/\sqrt{R_4} \) by a quarter-wave length. The latter impedance is inverted and the resulting reciprocal impedance is in parallel with the former impedance. Hence, parasitic effect cancellation and sheet resistance tolerance can be achieved similar to the proposed termination network for the coupler. In the ideal case, for perfect matching we should have

\[
Z_3 = \frac{R_3 R_4 Z_0}{\sqrt{R_3 - Z_0}}
\]

and for simplicity we choose \( R_3 = R_4 = 2Z_0 \) resulting in \( Z_3 = 2Z_0 \). This way, the resistors can be sized identically in the circuit layout which makes the resistor parasitic effects similar and is quite helpful if the resistor model is unknown. We note that within known parasitic effects, the values of \( Z_3, R_3 \), and \( R_4 \) can be optimized to achieve more bandwidth or a higher sheet resistance tolerance. Although \( Z_4 \) is insignificant for the response at the center frequency and can also be optimized to obtain more bandwidth, we select \( Z_4 = Z_2 = \sqrt{2}Z_0 \). Thus, impedances seen from the two ends of \( Z_3 \) are equalized and a better parasitic effect cancellation can be achieved by the symmetrical circuit.

The odd-mode impedance \( Z_o^W \) of a Wilkinson divider is \( \sqrt{2}T/(\rho/2+X/2) \), since we have a two times smaller resistor with a value of \( \rho/2 \) and we assume the associated normalized parasitic reactance is also half with a value of \( X/2 \). Therefore, at the center frequency, the odd-mode reflection coefficient is

\[
\lim_{T \to \infty} |\Gamma_o^W| = \lim_{T \to \infty} \left| \frac{Z_o^W - 1}{Z_o^W + 1} \right| = \left| \frac{\rho + X - 2}{\rho + X + 2} \right|
\]

which is the same for a Gysel divider as \( T \to \infty \). On the other hand, in our proposed divider, the odd-mode impedance \( Z_o^o \) becomes

\[
Z_o^o = \frac{Z_T}{2} \left( \frac{Z_T}{2} + j2T \right)
\]

where \( Z_T = \sqrt{2}T/(\rho + X) \). At the center frequency, odd-mode reflection coefficient of the proposed divider is

\[
\lim_{T \to \infty} |\Gamma_o^O| = \lim_{T \to \infty} \left| \frac{Z_T/\sqrt{4/Z_T} - 1}{Z_T/\sqrt{4/Z_T} + 1} \right| = \lim_{T \to \infty} |\Gamma_o^W|^2
\]

and hence twice the odd-mode reflection coefficient (in dB-scale) of a Wilkinson divider is achieved. An improvement in \( \Gamma_o \) significantly improves the output reflection and isolation coefficients of the divider since they are equal to \( |\Gamma_o/2 + \Gamma_e/2| \) and \( |\Gamma_o/2 - \Gamma_e/2| \), respectively, and \( \Gamma_e \) is small as it is a weak function of the resistor nonidealities.

Fig. 5a shows the odd-mode reflection coefficients \( \Gamma_o^o \) and \( \Gamma_o^W \) at the design center frequency \( f_0 \). For the Wilkinson and Gysel power dividers, 20 dB return loss is barely achieved when there is no variation in \( \rho \) for an \( |X_R| \) of only 0.2, while the proposed divider has a return loss better than 20 dB for \( \pm 30\% \) variation in \( \rho \) for an \( |X_R| \) up to 0.4. Also, the normalized 20 dB bandwidth is deteriorated much less compared to the conventional dividers as shown in Fig. 5b.

III. Fabrication and Experimental Results

A. Fabrication Technology and Experimental Setup

A Lange coupler with the proposed termination network and the presented power divider are designed at Ka-band and fabricated using our GaN-based microstrip technology. To test the tolerance to variations in resistor values, two more variants of
each design are also placed in the same reticle and fabricated in the same run. The additional coupler and divider variants use 30% smaller and 30% larger resistors compared to the original designs. Length of the resistors are kept unchanged whereas width of the resistors are varied in the test circuits.

The 100 μm-thick SiC substrate has a dielectric constant of 9.7. The process uses gold for metalization and TaN sputtering to form thin-film resistors. The topmost metal is 4 μm thick. Resistive elements are 90 nm thick with a sheet resistance of 30 Ω/□. For reference, quarter-wave length at 30 GHz is approximately 1.1 mm with this technology.

Three-port measurements are performed using Cascade1 RF wafer probe station, GGB2 GSG150 picoprobes and R&S3 ZVA40 vector network analyzer. The measurement results are in good agreement with our simulations, but slightly worse due to the actual process variations in addition to the deliberately modified resistor values.

B. Experimental Results

Width of the coupler fingers is 14 μm with 8 μm spacing between them. The termination network uses two 30 μm-wide high power shunt resistors of 75 Ω and 90 Ω separated by a meandered quarter-wave length transmission line with a characteristic impedance of 90 Ω. The resistors share the 85 μm-wide vias with the measurement pads. Size of the coupler does not increase with the modified termination network and is less than 0.8 mm × 1.55 mm including the 50 Ω feed lines and on-wafer measurement pads. Microscope photographs of the fabricated Lange couplers are shown in Fig. 6.

Fig. 7 shows the measured S-parameters of the fabricated couplers. Input reflection and transmission coefficients are similar in all variants as expected from equations (3)–(5). The nominal coupler achieves 20 dB input and output return losses and isolation from DC up to the maximum measurement frequency of 40 GHz. The coupled and direct powers are equal at 30.4 GHz with an extra insertion loss less than 0.45 dB, where the phase difference between the output ports is 91.7°.

The measured return loss and isolation levels in all coupler variants are better than 17 dB from 10.8 GHz to 40 GHz despite the 30% change in resistor values. The phase imbalances are within ±3° from 16.9 GHz to 40 GHz. The amplitude imbalances are less than 2 dB from 22 GHz to 40 GHz.

Widths of the quarter-wave length divider lines are 39 μm, 10 μm, and 55 μm with characteristic impedances of 71 Ω, 102 Ω, and 63 Ω. All resistors are 28.5 μm wide. The bridging resistor is 160 Ω and the shunt resistors are 96 Ω. Divider size including the 50 Ω feed lines and on-wafer measurement pads is less than 2.58 mm × 1.02 mm. Microscope photographs of the fabricated power dividers are shown in Fig. 8.

Fig. 9 shows the measured S-parameters of the fabricated dividers. The nominal divider achieves 20 dB input and output return losses and isolation from 19.7 GHz to 32.7 GHz with a fractional bandwidth of 50%.

When the resistor values are changed by ±30%, the lower frequency increases to 21.7 GHz, and a fractional bandwidth of 40% is maintained, demonstrating the tolerance to sheet resistance variance. Extra insertion losses are less than 0.4 dB in this band, and less than 0.25 dB at the center frequency.

A comparison with other quadrature couplers (QC) and power dividers (PD) is provided in Table I. This brief stands

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1 Cascade Microtech, Inc., Beaverton, OR, USA.
2 GGB Industries, Inc., Naples, FL, USA.
3 Rohde & Schwarz GmbH & Company KG, Munich, Germany.
The effect of nonideal resistors in splitting structures is analyzed. An isolation network technique is presented and used to design a Lange coupler and a power divider at Ka-band. High performance in a wide band is achieved while having a sheet resistance tolerance of 30%. Since the resistor parasitic effects increase with frequency the proposed method is quite useful for millimeter-wave circuits.

### REFERENCES


