



# On the elastic properties of INGaN/GaN LED structures

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Received: 24 October 2018 / Accepted: 9 January 2019 / Published online: 18 January 2019  
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## Abstract

In this study, three InGaN/GaN light-emitting diode (LED) structures with five periods are investigated grown by metal organic chemical vapor deposition (MOCVD) technique. During growth of these three samples, active layer growth temperatures are adjusted as 650, 667 and 700 °C. These structures are grown on sapphire (Al<sub>2</sub>O<sub>3</sub>) wafer as InGaN/GaN multi-quantum wells (MQWs) between *n*-GaN and *p*-AlGaN + GaN contact layers. During growth, pressure and flux ratio of all sources are kept constant for all samples. Only temperature of InGaN active layer is changed. These structures are analyzed with high-resolution X-ray diffraction (HR-XRD) technique. Their surface morphologies are investigated with atomic force microscopy (AFM). Reciprocal space mapping (RSM) is made different from classical HR-XRD analyses. Using this method, mixed peaks belonging to InGaN, AlGaN and GaN layers are seen more clearly and their full width at half maximum (FWHM) values is determined with better accuracy. With FWHM gained from RSM and Williamson–Hall (W–H) method based on universal elastic coefficients of the material, particle size *D* (nm), uniform stress  $\sigma$  (GPa), strain  $\epsilon$  and anisotropic energy density  $u$  (kJ m<sup>-3</sup>) parameters for the samples are calculated. The results are compared with literature. On the other hand, to have an idea about the accuracy of the results AFM images are examined. Parameters calculated showed differences but it is seen that the largest particle size is gained for GaN and the smallest is gained for AlGaN. For all parameters, it is seen that they increase for GaN layer and decrease for AlGaN layer with increasing temperature. For InGaN layer parameters, they showed both increasing and decreasing or decreasing and increasing behavior harmonically with an increase in temperature. Results showed that they are compatible with literature. Results gained from Scherrer and W–H are very near to each other.

## 1 Introduction

Aim of this study is to investigate the elastic properties of In<sub>x</sub>Ga<sub>1-x</sub>N/GaN MQW LED structures grown by MOCVD with RSM and effects of these properties on the performance of such devices.

Optoelectronic devices with nitrides have great importance in nanotechnology. Direct band gaps of InN, GaN and AlN are 0.7, 3.4 and 6.2 eV, respectively. These band gaps are in near infrared to ultraviolet region in electromagnetic spectrum [1]. With such properties, semiconductors with nitrides have importance in the development of devices

such as LEDs, laser diodes, microchips and photo detectors. These semiconductors with nitrides can operate in hard conditions as high pressure and temperature, and this is a good advantage [2]. InGaN LEDs have resistivity against high temperature, pressure and frequency. These structures are grown on silicon (Si) or sapphire (Al<sub>2</sub>O<sub>3</sub>) wafers traditionally. This growth causes cracks in the layers. The reason for these cracks is the lattice mismatch. This mismatch causes dislocations and the density of these dislocations is between 10<sup>7</sup> and 10<sup>11</sup> cm<sup>-2</sup> [3, 4]. In these types of structures, structural defects can often be seen. To remove these defects, GaN buffer layer is grown between sapphire and InGaN/GaN active quantum well layer. This operation eliminates the lattice mismatch that will be transferred to InGaN layer but it does not completely remove the lattice mismatch. Because of the mismatch between sapphire and GaN layer in the percentage of 15%, the transfer of threatening dislocations (TD) to InGaN active layer between the densities of 10<sup>8</sup>–10<sup>12</sup> cm<sup>-2</sup> is inevitable [5, 6]. Although there are such negative properties, devices formed by semiconductors with nitrides have better performance [6].

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In this study, three InGaN MQW LED structures are investigated which are grown on (001) oriented sapphire wafer. All the parameters except growth temperature are kept constant during growth. To examine the structural properties of the samples in more detail, diffraction pattern gained from HR-XRD is used. These patterns are transformed to RSM for symmetric and asymmetric planes. By the help of this method, defects in the structures are seen more clearly. In the calculations of this study cubic equation is used [7].

## 2 Experimental details

In this study, InGaN/GaN MQW LED samples are grown with AIXTRON RF200/4 RF-S MOCVD system. InGaN, GaN and AlGaN layers are grown on c-(001)-oriented sapphire substrate. Before the epitaxial growth operation, sapphire substrate is exposed to temperature of 1100 °C in nitrogen atmosphere for 10 min to remove the oxide layer on the surface of it [8, 9]. Trimethylgallium (TMGa), trimethylaluminum (TMAI), trimethylindium (TMIn) and ammonia (NH<sub>3</sub>) compound chemical reactions are gained from Ga, Al, In and N sources, respectively. At 200 mbar pressure and at 500 °C temperature, GaN nucleation layer is grown on sapphire substrate [10]. Later at 1020 °C temperature, GaN buffer layer is grown. An n-type GaN contact layers are grown at 1030 °C with constant 23 sccm TMGa flux ratio. First layer of this contact layer is grown for 35 min and second layer is grown for 20 min. In 140 sccm TMGa and TMIn flux ratio, InGaN active layer of the samples A, B and C is grown at 650, 667, 700 °C, respectively, with a duration of first 90 s and later 390 s as five layers. Over these active layers, in 140 sccm TMGa flux ratio GaN cap layer is grown for 390 s at 730 °C. p-Contact AlGaN layer with

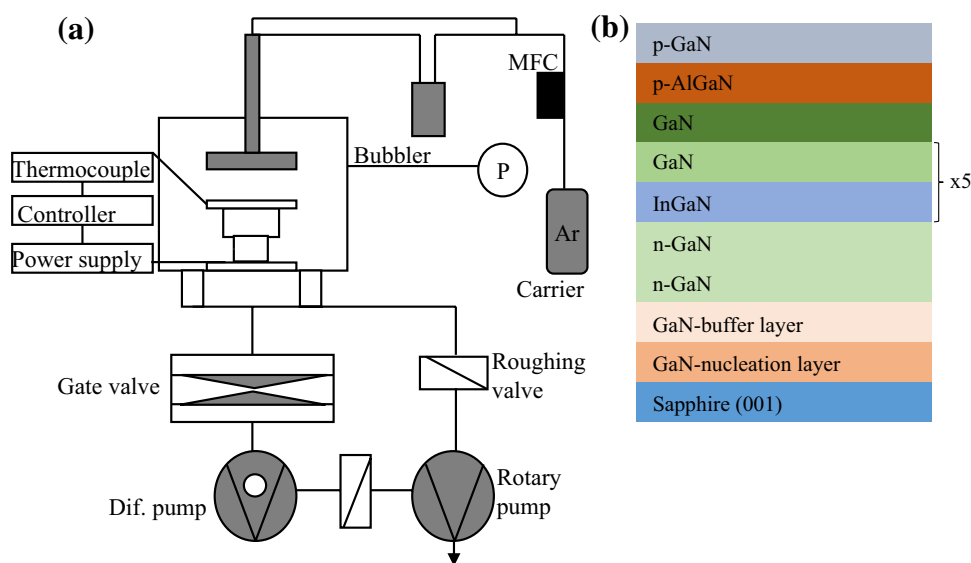
magnesium (Mg) deposition is grown for 65 s using 9 sccm TMGa, 15 sccm TMAI and 90 sccm Cp<sub>2</sub>Mg flux ratio. During this operation, temperature is kept constant at 1085 °C and pressure is kept constant at 50 mbar. p-GaN layer is grown with 14 sccm TMGa and 100 sccm Cp<sub>2</sub>Mg flux ratio at 1010 °C and 200 mbar for 720 s. NH<sub>3</sub> flux ratio is 1300 sccm for GaN, AlGaN layers and 5200 sccm for InGaN/GaN active layer (Fig. 1).

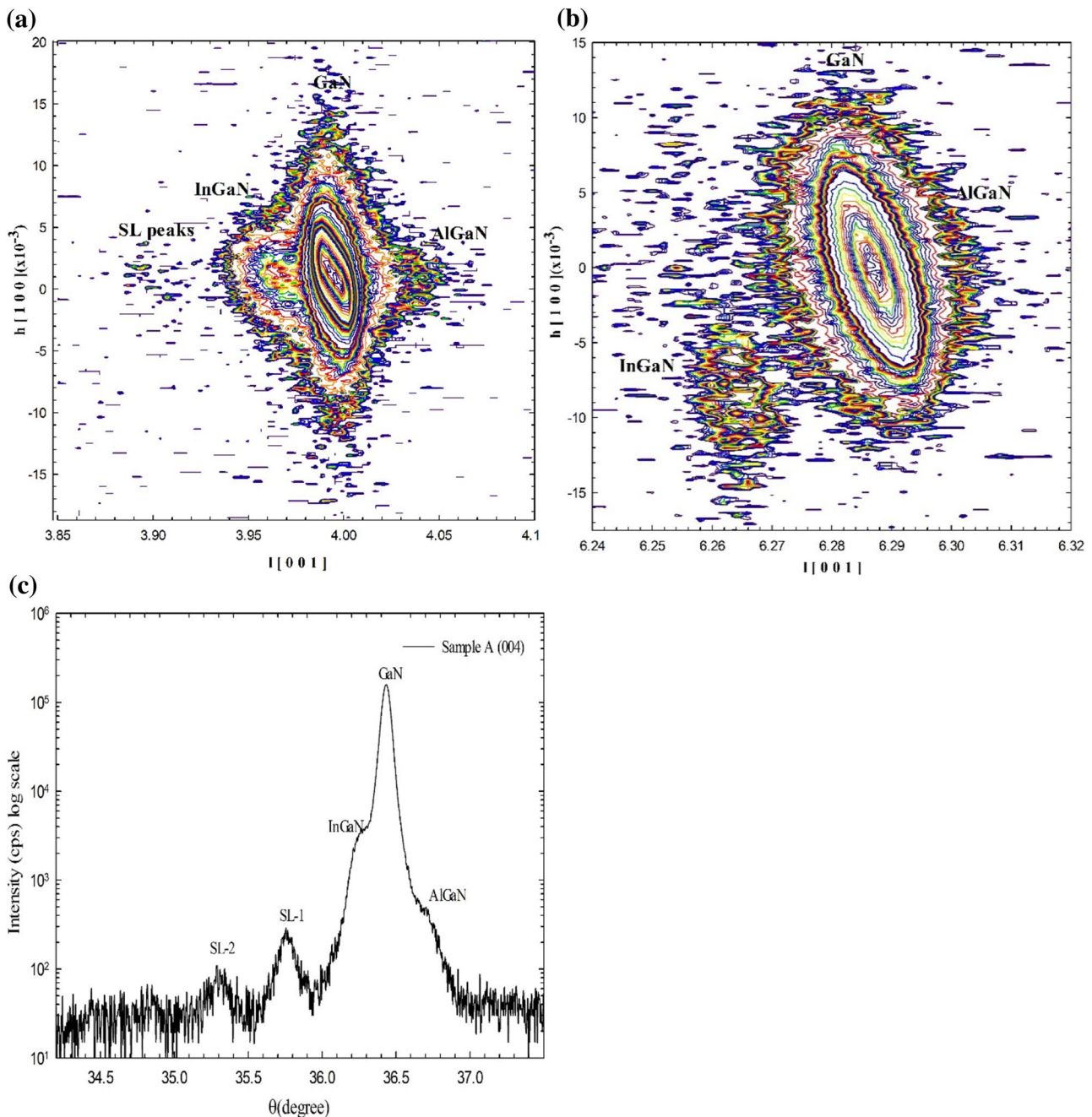
## 3 Results and discussion

In this study, particle size *D* (nm), uniform stress  $\sigma$  (GPa), strain  $\epsilon$ , and anisotropic energy density *u* (kJ m<sup>-3</sup>) parameters are calculated using RSM method. In classical calculations, 2 $\theta$  diffraction angle is kept constant in diffraction plane and rocking curve results gained by detecting the  $\theta$  angle are used often in literature [11–13]. Bruker axS D8 Discover brand HR-XRD device was used for XRD measurements.

Patterns gained from RSM are clearer than classical HR-XRD peaks [2]. Mixed GaN, InGaN and AlGaN layer peaks can be distinguished from each other by the help of RSM. The comparison of classical HR-XRD pattern for samples A, B and C for (004) symmetric plane is given in Figs. 2, 3 and 4c and RSM of them is given in Figs. 2, 3 and 4a. If Fig. 2c is examined carefully, on the right of GaN peak AlGaN peak is not fully distorted but it can be seen in Fig. 2a clearly on the right of GaN peak. Again in the same figures, InGaN peak can be seen clearly on the right of GaN peak. By the help of RSM, satellite peaks (SL) can also be determined clearly. Generally, for RSM InGaN, GaN and AlGaN peaks are scanned for wide offset values and later these offsets are eliminated according to universal values of GaN. RSM

**Fig. 1** a The schematic diagram of the experimental installation for the MOCVD system. b Schematic view of InGaN/GaN LED structure



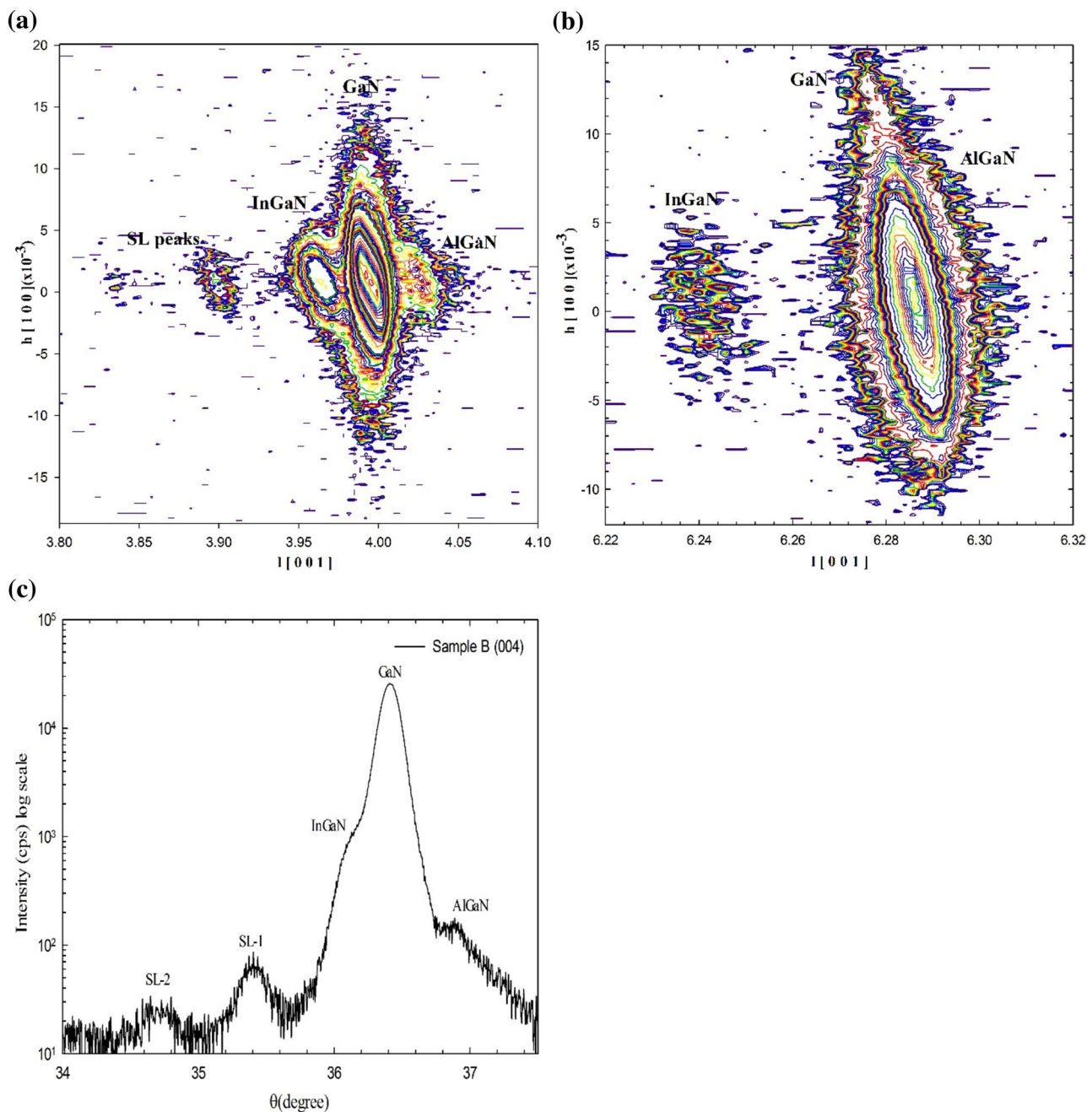


**Fig. 2** **a** RSM of sample A in (004) symmetric plane. **b** RSM of sample A in (106) asymmetric plane. **c** XRD of sample A in (004) symmetric plane

pattern of sample A for symmetric (004) miller reflection plane is given in Fig. 2a. If this figure is examined carefully, on the right of the figure sapphire peak can be seen, and InGaN and AlGaN peaks can be seen mixed in GaN peak.

In Fig. 2b, RSM image of sample A for (106) asymmetric plane can be seen. If this image is examined, InGaN partly distorted from GaN and AlGaN not fully distorted can be seen. RSM image of sample B for symmetric (004)

miller reflection plane is given in Fig. 3a. If this figure is examined SL-1 and SL-2 satellite peaks can be seen together and InGaN, AlGaN peaks can be seen as more distorted from each other according to sample A. Here symmetric peaks are more dominant in (004) plane. Interference of incident reflections caused from density difference of GaN and InGaN layers forms these satellite peaks. These satellite peaks are related with crystal quality and

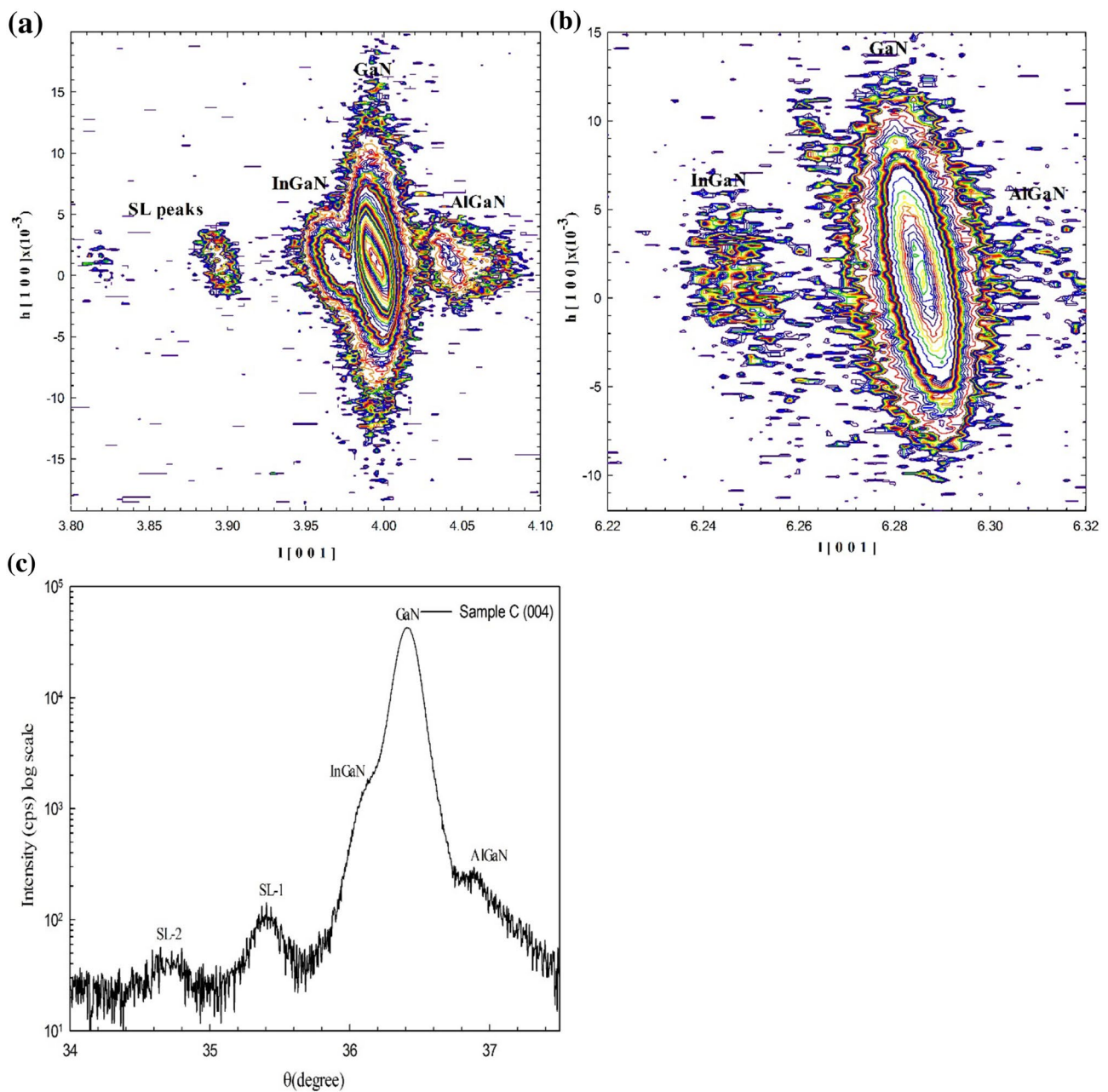


**Fig. 3** **a** RSM image of sample B in (004) symmetric plane. **b** RSM image of sample B in asymmetric (106) plane. **c** XRD of sample B in (004) symmetric plane

surface roughness of inter-layers. They are used for determining multi-quantum well thickness. Thickness calculation can be made with the formula of  $T = \lambda / (2\Delta\theta \cos \theta)$  [14]. Here  $\lambda$  is the wavelength,  $\Delta\theta$  is the SL distortion and  $\theta$  is the Bragg angle of the plane. RSM image of sample B for (106) reflection plane is given in Fig. 3b. If this figure is examined carefully, it can be seen that InGaN layer is distorted from GaN clearly but not fully distorted from AlGaN.

RSM images of sample C are given in Fig. 4a, b for symmetric and asymmetric planes. If the pattern for (004) symmetric plane is examined, it can be seen that SL-1 and SL-2 peaks are distorted from each other clearly. In the same pattern, InGaN peaks are less distorted and AlGaN peaks are more clearly distorted.

In (106) asymmetric plane RSM image, just like in symmetric plane images InGaN peaks are clear but AlGaN peaks are not clear and GaN peaks are partly formed. If



**Fig. 4** **a** RSM image of sample C in (004) symmetric plane. **b** RSM image of sample C in (106) asymmetric plane. **c** XRD of sample C in (004) symmetric plane

Figs. 2, 3 and 4 are examined carefully again SL peaks are not seen for sample A but for samples B and C SL-1 and SL-2 satellite peaks are seen distorted from each other and more clearly. The reason for this maybe that on increasing of roughness for inter-layers, XRD interferences deteriorate. Missing of SL-2 satellite peak in sample A shows that crystal quality is low and there is big roughness between layers in this sample. Distortion of satellite peaks clearly from each other in samples B and C indicates that there is

good crystal quality and less roughness in these samples. As a result, better crystal quality is observed at 667 and 700 °C growth temperatures. Distortion of InGaN peak in sample B causes from increasing of In ratio in this compound. Distortion of AlGaN peak more clearly indicates that Al ratio in the compound is more than in sample B [15]. Bad distortion of HR-XRD peaks for InGaN and AlGaN is related with microstructural defects in these samples [16].

### 3.1 Particle size calculation according to Scherrer method

To apply Scherrer method healthily, calculation of FWHM accurately is important [17].

Bragg peak patterns gained from HR-XRD analyses is dependent on both device and sample effects. Modified FWHM corresponding to every InGaN diffraction peak is given with Eq. (1):

$$\beta_{hkl}^2 = \beta_S^2 + \beta_D^2 \tag{1}$$

Particle size normal to the reflection planes D is given as

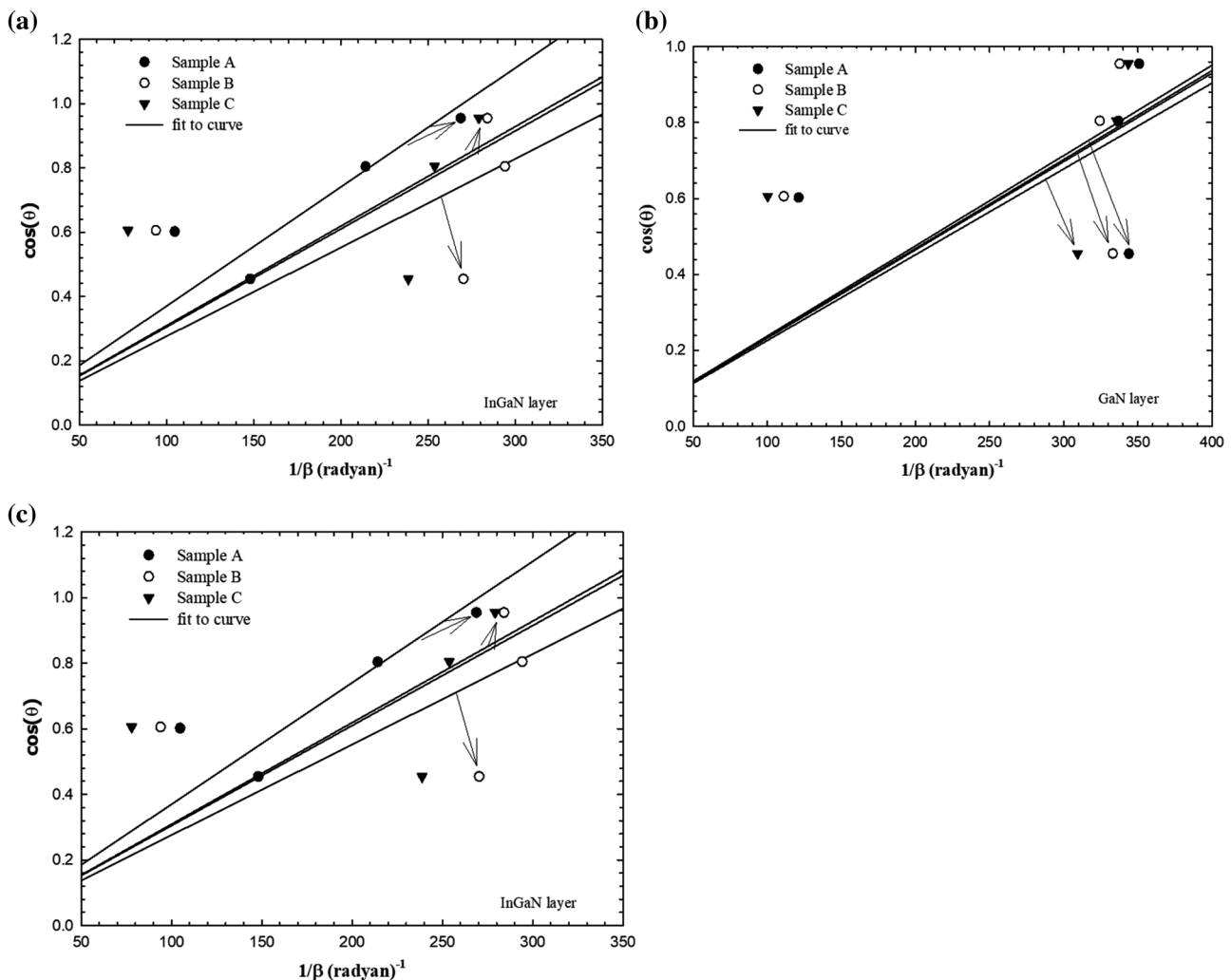
$$D = \frac{k\lambda}{\beta_{hkl} \cos \theta} \rightarrow \cos \theta = \frac{k\lambda}{D} \left( \frac{1}{\beta_{hkl}} \right) \tag{2}$$

Here  $k$  is a constant,  $\lambda$  is the X-ray wavelength and  $\theta$  is Bragg angle. By fitting the data, slope of the fit gives particle size  $D$ . Using FWHM ( $\beta_{hkl}$ ) values gained from RSM,  $\cos\theta$  versus

$1/\beta_{hkl}$  Scherrer plot is drawn for InGaN active layer. This plot can be seen in Fig. 5a. In Fig. 5b, c, Scherrer plots for GaN and AlGaN can be seen, respectively. By the slope of the fits in these plots  $D$  particle size is calculated in nm. According to these calculations, particle sizes for InGaN, AlGaN and GaN are found as 35.895, 21.773 and 51.326 nm, respectively.

### 3.2 Particle size calculation according to W–H method

In reality not all the materials are crystalized. They mostly have deformation in their structures. Strain is a defect that comes out by the imperceptivity of the crystal or lattice mismatch. It can be calculated as  $\epsilon \approx \beta s / 4 \tan \theta$ . In the diffraction pattern, displacement of the peak causes variation in FWHM. For calculation of strain, it is thought as a linear equation as  $y = a \times x$ .  $\tan \theta$  versus  $\beta_{hkl}$  line is plotted. When this plot is fitted slope gives us  $1/\epsilon$ . Inverse of this expression mathematically gives



**Fig. 5** a Scherrer plot ( $\beta_{hkl}^{-1}/\cos\theta$ ) of InGaN layers for samples A, B and C. b Scherrer plot ( $\beta_{hkl}^{-1}/\cos\theta$ ) of GaN layers for samples A, B and C. c Scherrer plot ( $\beta_{hkl}^{-1}/\cos\theta$ ) of AlGaN layers for samples A, B and C

strain. This result is also not as realistic as in particle size calculation. However, W–H method is a technique that distinguishes these two effects and it is compatible with the experimental method. It is useful to mention three methods used as W–H method. In this study W–H calculations are made according to three models. They are: uniform deformation model (UDM), uniform stress deformation model (USDm) and uniform deformation energy density model (UEDDM), respectively. W–H model is not dependent on  $1/\cos\theta$  as in Scherrer model but it changes with  $\tan\theta$ . This basic difference is used for distinguishing micro-strain and reflection broadening [17]. Strain is caused from imperceptivity of the crystal and separation. It can be calculated with Eq. (3) [18]. Here  $\epsilon$  is the square root of the mean square (RMS) value:

$$\epsilon = \frac{\beta_{hkl}}{4 \tan \theta}. \tag{3}$$

Figure 6a–c shows  $\tan\theta$  versus  $\beta_{hkl}$  plots for InGaN, GaN and AlGaN layers, respectively.

Strain and particle size are not independent of each other linearly. For this reason, peak width of Bragg reflections is given as the sum of the peak widths coming from two effects. Contribution of particle size and strain to line broadening are thought as independent of each other and by assuming that they both have a Cauchy-like profile, line width is the sum of two terms. This is given in the following equations:

$$\beta_{hkl} = \beta_1 + \beta_\epsilon = [K\lambda/t \cos \theta_{hkl}] + [4\epsilon \tan \theta_{hkl}], \tag{4}$$

$$\beta_{hkl} \cos \theta_{hkl} = \beta_1 + \beta_\epsilon = [K\lambda/t] + [4\epsilon \sin \theta_{hkl}]. \tag{5}$$

This equation is known as classical W–H equation or uniform deformation model (UDM). According to this equation strain is the same in all directions. For this reason crystal is thought to be isotropic. On the other hand UDM is not dependent on direction. If  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4\sin\theta_{hkl}$  is plotted using the miller planes of the crystal, slope gives the micro-strain  $\epsilon$ . Intercept of y-axis gives the particle size. Calculated values are given in Tables 3, 4 and 5. For all three samples plots are given in Fig. 7a–c.

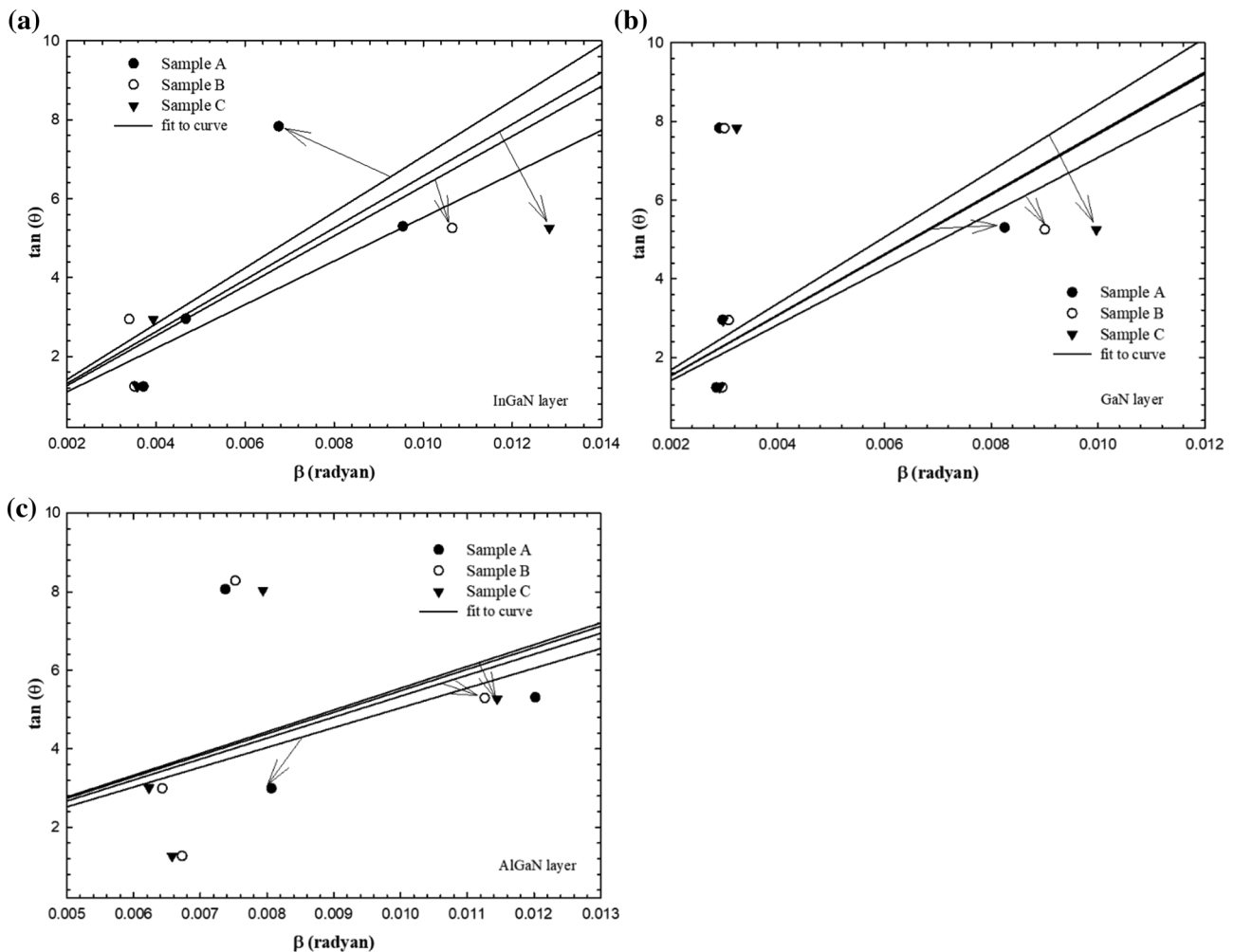


Fig. 6 a InGaN layers  $\tan\theta$  versus  $\beta_{hkl}$  plots. b GaN layers  $\tan\theta$  versus  $\beta_{hkl}$  plots. c AlGaN layers  $\tan\theta$  versus  $\beta_{hkl}$  plots

Because of the produced high pressure, diffraction line broadens and makes a shift to a bigger  $d$  space. This shows the stress in InGaN lattice. Positive strain value gained from  $\beta_{hkl}\cos\theta_{hkl}$  versus  $4\sin\theta_{hkl}$  plot supports the presence of stress. In many situations, acceptance of homogeneity and isotropy is not true. For this reason, USDM and UDEDM methods are better methods because they take into account of Young modulus [19].

According to USDM method, the reason for anisotropic micro-strain ( $\epsilon_{hkl}$ ) is uniform deformation stress ( $\sigma$ ). Hooke's law related with strain describes the direct proportion between stress and strain as  $\sigma = \epsilon E_{hkl}$ . Using this approximation W-H equation can be written as Eq. (6) [16]:

$$\beta_{hkl} = \left(\frac{k\lambda}{D}\right) + \left(\frac{4\sigma \sin\theta}{E_{hkl}}\right). \tag{6}$$

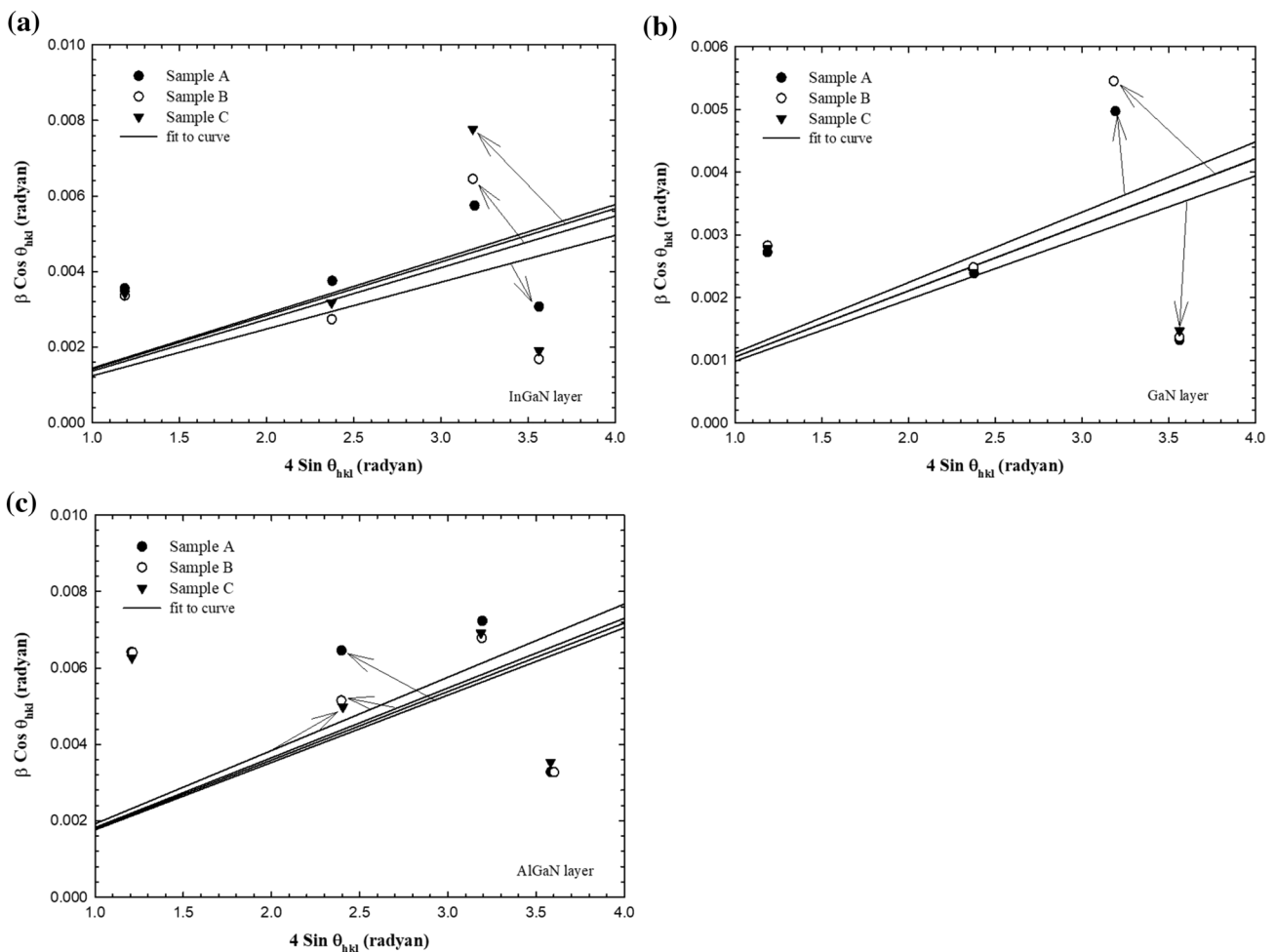
$$E_{hkl} = \left(h^2 + \frac{(h+2k)^2}{3} + \left(\frac{al}{c}\right)^2\right)^2 \cdot \left[ s_{11} \left(h^2 + \frac{(h+2k)^2}{3}\right) + s_{33} \left(\frac{al}{c}\right)^4 + (2s_{13} + s_{44}) \left(\left(h^2 + \frac{(h+2k)^2}{3}\right) \left(\frac{al}{c}\right)^2\right) \right]^{-1}. \tag{8}$$

Here  $E_{hkl}$  is the Young modulus which is normal to the  $hkl$  planes. Stress can be found by the slope of the  $4\sin\theta/E_{hkl}$  versus  $\beta_{hkl}\cos\theta$  plot. Particle size can be determined by the interception point of the fit of this plot [17].

Elastic parameters of InN and GaN found in InGaN compound are given in Table 1. Elastic coefficients of InGaN can be calculated using Vegard's law. Samples A, B and C have in ratios of 0.109, 0.090 and 0.080, respectively. Vegard's law is given as

$$c_0(\text{InGaN}) = x c_0(\text{InN}) + (1-x) c_0(\text{GaN}). \tag{7}$$

Young modulus for a hexagonal shaped crystal is given as [20, 21]:



**Fig. 7** **a** InGaN layers  $\beta_{hkl}\cos\theta_{hkl}$  versus  $4\sin\theta_{hkl}$  plots. **b** GaN layers  $\beta_{hkl}\cos\theta_{hkl}$  versus  $4\sin\theta_{hkl}$  plots. **c** AlGaIn layers  $\beta_{hkl}\cos\theta_{hkl}$  versus  $4\sin\theta_{hkl}$  plots



**Table 1** Universal elastic coefficients of InGaN for all three samples

	InN	GaN	InGaN		
			A	B	C
$C_{11}$	190	390	368.26	371.98	374.98
$C_{12}$	104	145	140.54	141.31	141.92
$C_{13}$	121	106	107.63	107.35	107.13
$C_{33}$	182	398	374.52	378.54	381.78
$C_{44}$	10	105	94.67	96.44	97.87

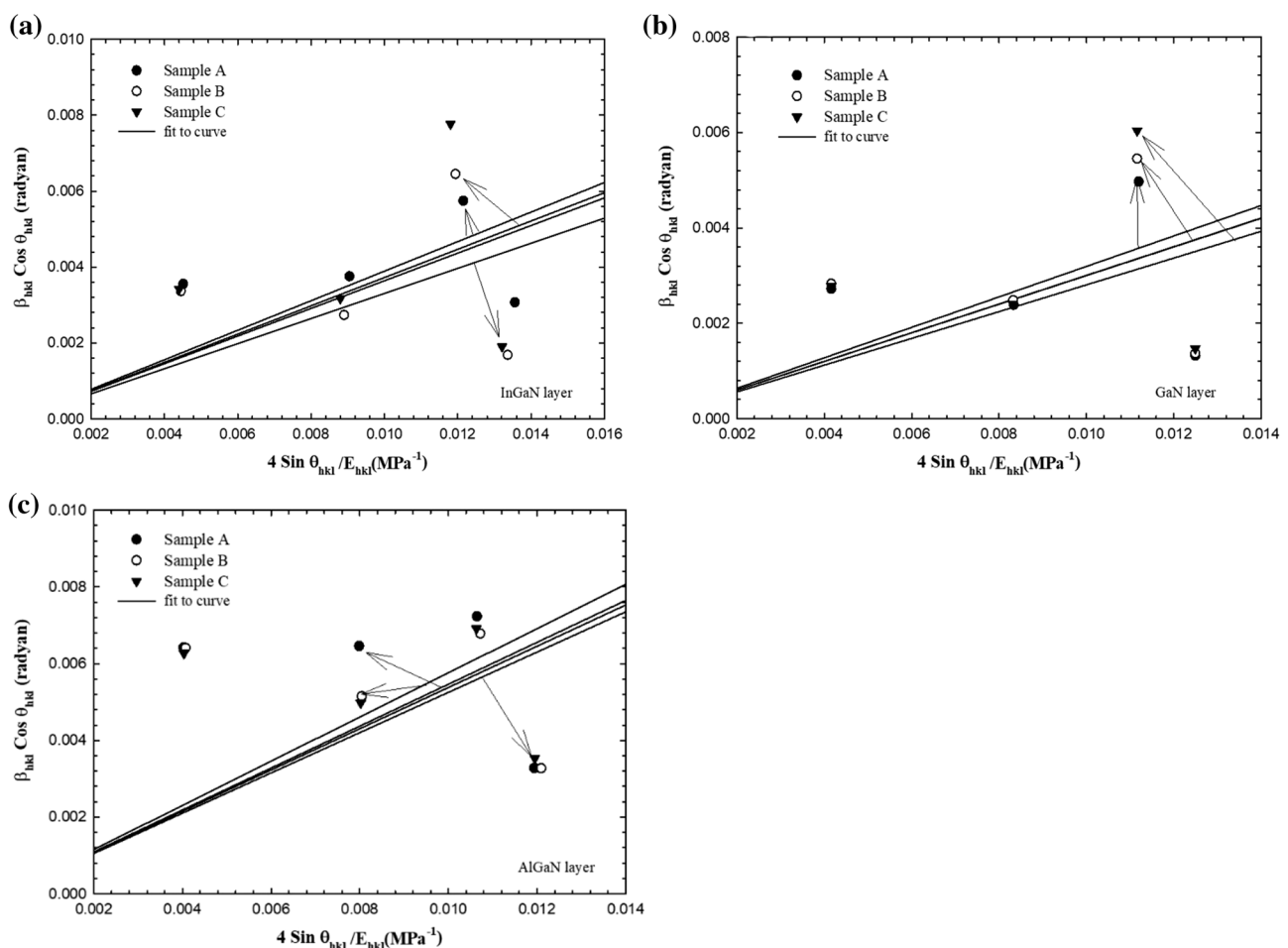
**Table 2** Elastic compliances for InGaN and AlGaN

	(Gpa <sup>-1</sup> )					
	A		B		C	
	InGaN	AlGaN	InGaN	AlGaN	InGaN	AlGaN
$S_{11}$	0.0033	0.0030	0.0033	0.0030	0.0032	0.0030
$S_{12}$	0.0011	0.0010	0.0011	0.0010	0.0011	0.0010
$S_{13}$	0.0006	0.0005	0.0006	0.0005	0.0006	0.0005
$S_{33}$	0.0030	0.0028	0.0030	0.0028	0.0030	0.0028
$S_{44}$	0.0106	0.0086	0.0104	0.0087	0.0102	0.0086

Here  $s_{11}$ ,  $s_{12}$ ,  $s_{13}$ ,  $s_{33}$ , and  $s_{44}$  are elastic coefficients for InGaN and AlGaN, and they are given in Table 2.

Figure 8a–c shows  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta_{hkl} / E_{hkl}$  plots for all three samples for InGaN, AlGaN and GaN according to USDM method.

Another model in W–H is USDEM. According to this model, the reason for strain is the deformation energy density. According to Hooke’s law,  $u$  is the energy density as a



**Fig. 8** a  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta_{hkl} / E_{hkl}$  plots for InGaN layers according to USDM model. b  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta_{hkl} / E_{hkl}$  plots for GaN layers according to USDM model. c  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta_{hkl} / E_{hkl}$  plots for AlGaN layers according to USDM model

function of strain. It may be given as  $u = \epsilon^2 E_{hkl} / 2$ . So Eq. (6) can be modified [17]

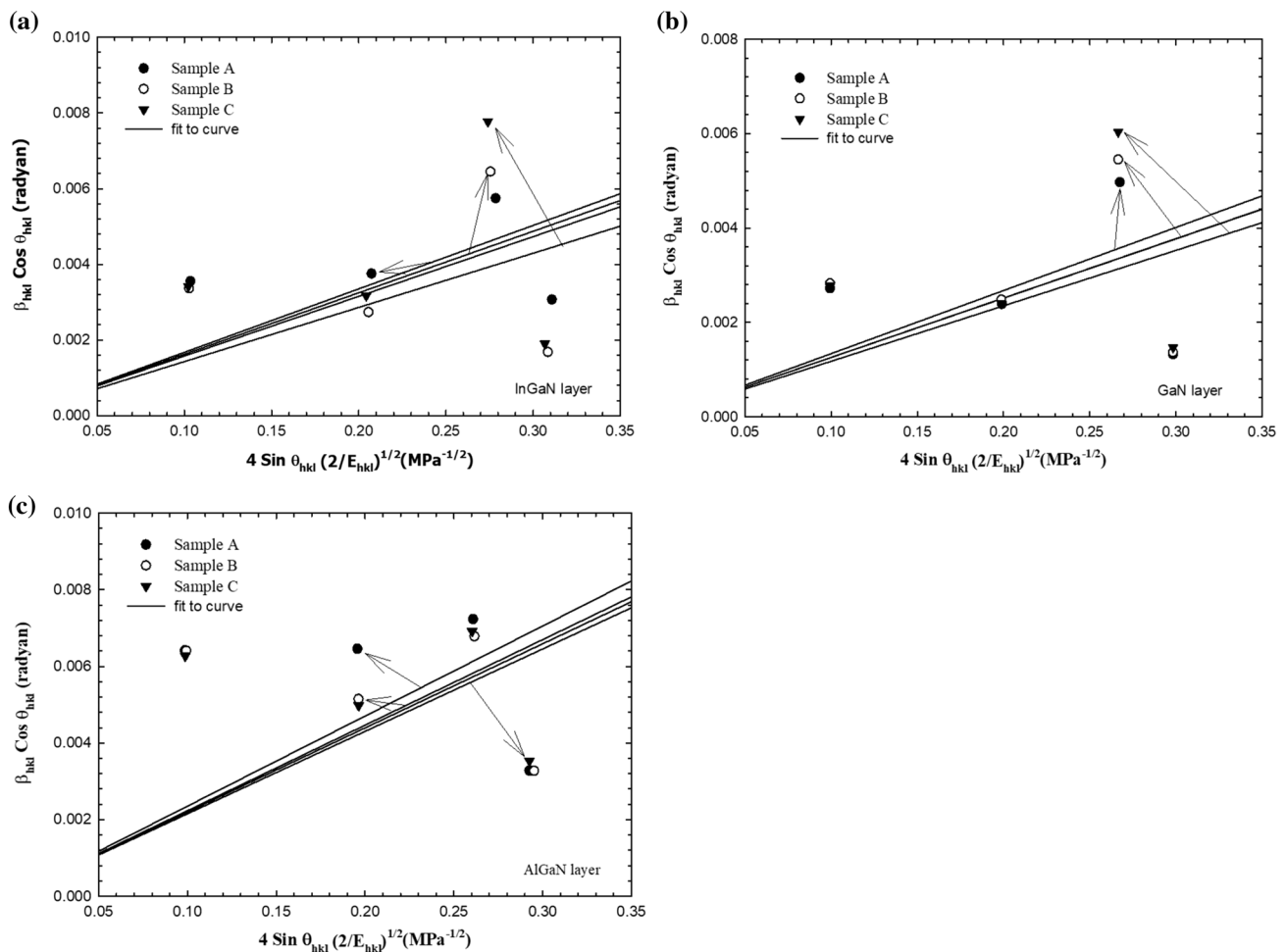
$$\beta_{hkl} = \left( \frac{k\lambda}{D} \right) + \left( 4 \sin \theta \left( \frac{2u}{E_{hkl}} \right)^{1/2} \right). \quad (9)$$

Figure 9a–c shows  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta (2u/E_{hkl})^{1/2}$  plots for InGaN, AlGaIn and GaN, respectively. If these plots are fitted, the slope of the fit gives anisotropic energy density ( $u$ ) and y-axis intercept gives particle size ( $D$ ). Deformation stress and deformation energy density can be related with each other as  $u = \sigma^2 / 2E_{hkl}$  in USDM and UDEDM models [17]. Equations (7) and (8) are different because they take into account the anisotropic elastic coefficients. In Eq. (7), deformation stress is the same in all directions and this situation makes  $u$  anisotropic.

In Eq. (8), deformation energy is accepted as uniform in all directions. Here deformation stress  $\sigma$  is taken as

anisotropic. For this reason, different values for strain and particle size can be found from these two equations. In Tables 3, 4 and 5, results gained from UDM, USDM and UDEDM, and Scherrer are listed for InGaN, AlGaIn and GaN layers of samples.

Results showed that strain is less effective on particle size [22]. If Tables 3, 4 and 5 are examined carefully, particle sizes gained from Scherrer and W–H can be compared. On the other hand, UDM, USDM and UDEDM methods gave similar results because the three methods are based on the W–H method. Young’s modulus results from the harmony between Hooke’s Law and anisotropic energy density. The same results were obtained because the  $a$ - and  $c$ -lattice parameters were used in the Young module. Strain in big angles results in the broadening of the peaks and particle size decrease. This situation is caused by increasing of reflection angles [22].



**Fig. 9** **a**  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta (2u/E_{hkl})^{1/2}$  plots for InGaN layers according to UDEDM model. **b**  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta (2u/E_{hkl})^{1/2}$  plots for GaN layers according to UDEDM model. **c**  $\beta_{hkl} \cos \theta_{hkl}$  versus  $4 \sin \theta (2u/E_{hkl})^{1/2}$  plots for AlGaIn layers according to UDEDM model

**Table 3** Physical parameters calculated for all three layers of sample A according to USD, USDM and UDEDM models

$\epsilon \times 10^{-3}$	Scherrer–W–H method											
	$D$ (nm) $\cos \theta$		$D$ (nm) $\sin \theta$	UDM		USDM			UEDDM			
				$D$ (nm)	$\epsilon \times 10^{-3}$	$D$ (nm)	$\sigma$ (Gpa)	$\epsilon \times 10^{-3}$	$D$ (nm)	$u$ (kJm <sup>-3</sup> ) $\times 10^3$	$\sigma$ (Gpa)	$\epsilon \times 10^{-3}$
InGaN	7.334	36.087	35.895	47.542	0.250	47.542	0.066	0.250	47.542	0.008	0.066	0.250
AlGaN	36.872	7.366	21.773	14.031	2.997	14.031	0.900	2.997	14.031	1.348	0.900	2.997
GaN	4.351	61.232	51.326	57.597	0.021	57.597	0.006	0.021	57.597	0.000	0.006	0.021

**Table 4** Physical parameters calculated for all three layers of sample B according to USD, USDM and UDEDM models

$\epsilon \times 10^{-3}$	Scherrer–W–H method											
	$D$ (nm) $\cos \theta$		$D$ (nm) $\sin \theta$	UDM		USDM			UEDDM			
				$D$ (nm)	$\epsilon \times 10^{-3}$	$D$ (nm)	$\sigma$ (Gpa)	$\epsilon \times 10^{-3}$	$D$ (nm)	$u$ (kJm <sup>-3</sup> ) $\times 10^3$	$\sigma$ (Gpa)	$\epsilon \times 10^{-3}$
InGaN	6.123	48.362	41.134	48.947	0.104	48.947	0.028	0.104	48.947	0.001	0.028	0.104
AlGaN	42.704	6.319	21.780	15.019	2.815	15.019	0.838	2.815	15.019	1.180	0.838	2.815
GaN	4.555	58.651	49.270	56.266	0.066	56.266	0.019	0.066	56.266	0.001	0.019	0.066

**Table 5** Physical parameters calculated for all three layers of sample C according to USD, USDM and UDEDM models

$\epsilon \times 10^{-3}$	Scherrer–W–H method											
	$D$ (nm) $\cos \theta$		$D$ (nm) $\sin \theta$	UDM		USDM			UEDDM			
				$D$ (nm)	$\epsilon \times 10^{-3}$	$D$ (nm)	$\sigma$ (Gpa)	$\epsilon \times 10^{-3}$	$D$ (nm)	$u$ (kJ m <sup>-3</sup> ) $\times 10^3$	$\sigma$ (Gpa)	$\epsilon \times 10^{-3}$
InGaN	6.042	43.723	38.965	51.325	0.361	51.325	0.097	0.361	51.325	0.018	0.097	0.361
AlGaN	49.670	5.468	21.899	15.414	2.723	15.414	0.816	2.723	15.414	1.112	0.816	2.723
GaN	4.790	55.718	48.625	62.418	0.230	62.418	0.066	0.230	62.418	0.008	0.066	0.230

**Table 6** Surface roughness values for three samples

Sample	RMS (nm)
A	2.07
B	9.55
C	2.31

### 3.3 Morphological properties of InGaN/GaN MQW blue LEDs

The morphological properties of the surface were characterized by high-performance Nano magnetic Pro-AFM atomic force microscopy (AFM) in dynamic scanning mode. Table 6 gives surface roughness values for three samples. Figure 10a–c shows a 3D AFM image of samples A, B and C at a scanning area of  $5 \times 5 \mu\text{m}^2$  at 650, 667 and 700 °C, respectively. Table 6 gives the surface roughness values for three samples. If the shape is carefully examined for sample A, cylindrical island formation is clearly visible. The B sample has better surface morphology than the other samples

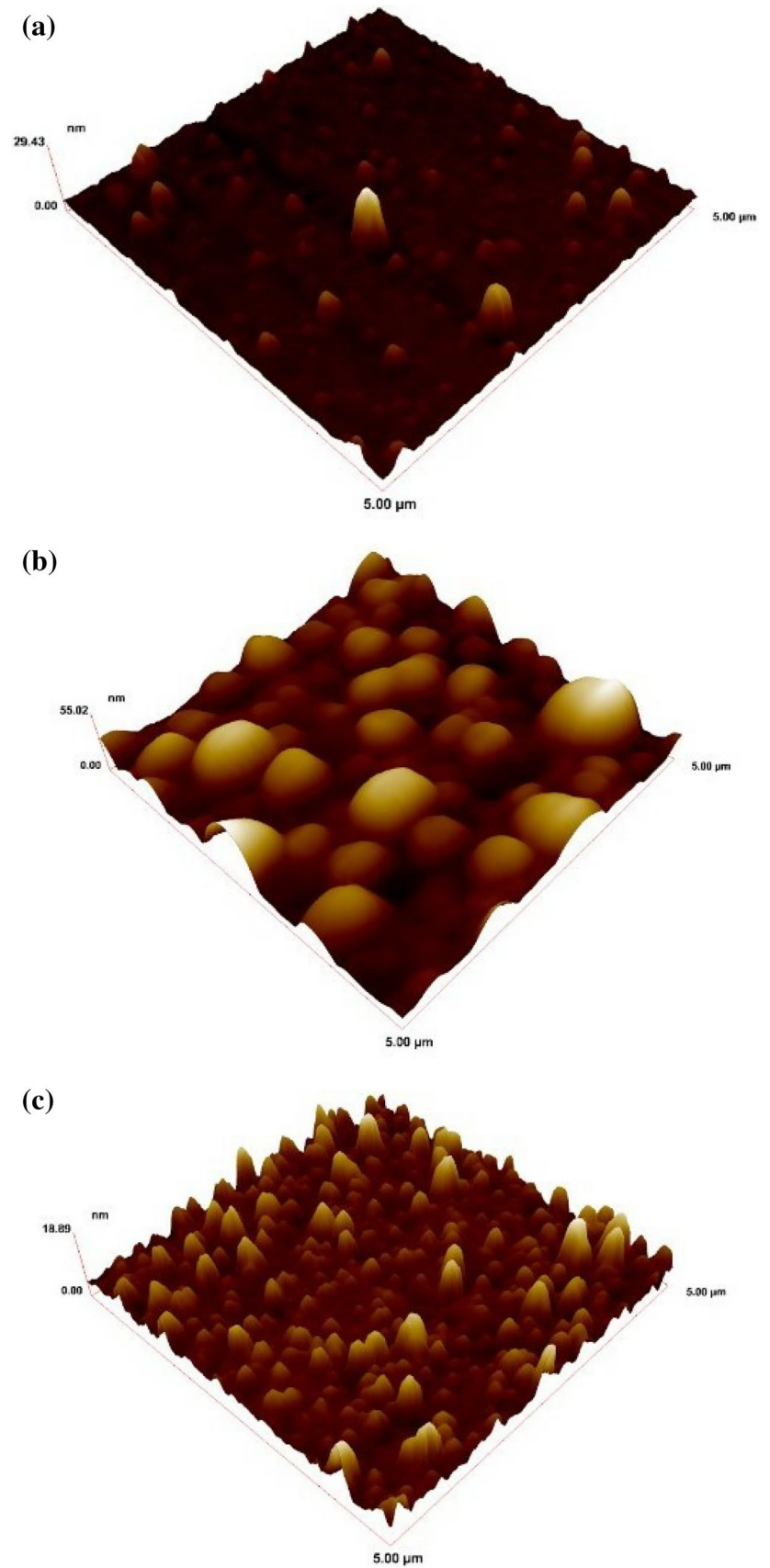
and is more homogeneous. Furthermore, the B sample has large particle shapes instead of cylindrical islands. Sample C consists of cylindrical islands as in sample A and has more surface roughness compared to sample B.

Variation of particle size is related with RMS value variations. These results are in accordance with the results gained from W–H. Also, surface morphology of samples A, B and C are like GaN structures grown by MOCVD in literature [21]. AFM results showed that surface morphology of InGaN/GaN LED structures is strongly affected by the growth temperature.

### 4 Conclusion

In this study, three samples of InGaN/GaN LED structures are grown by MOCVD method at 650, 667 and 700 °C active layer growth temperatures. These structures are characterized by HR-XRD method. Different from classical HR-XRD method, reciprocal space mapping technique is used. Using

**Fig. 10** **a** 3D AFM image of sample A. **b** 3D AFM image of sample B. **c** 3D AFM image of sample C



this technique, mixed InGaN, AlGaN and GaN peaks are determined more clearly and  $\beta_{hkl}$  values are determined with better accuracy. With the increase of the temperature in the plane 106, the relaxation status of the InGaN from the RSM for the three samples created a strain in the “*l*” direction. While the inverse space points of AlGaN and GaN coincide, the crystallinity of the increased temperature is distorted in the “*l*” direction.

In direction 004, the orientation of AlGaN in the “*l*” direction is clearly seen with increasing temperature. InGaN’s “*l*” direction shows increased strain in FWHM.  $\beta_{hkl}$  values gained from reciprocal space mapping and universal elastic coefficients of the material are used in W–H method to determine particle size (*D*), uniform stress  $\sigma$  (GPa), strain  $\varepsilon$  and anisotropic energy density  $u$  (kJ m<sup>-3</sup>). The results for these parameters are compared with literature.

As the result of the calculations, according to Scherrer method, InGaN particle size values first increase and later decrease with increasing temperature. The same value decreases continuously for AlGaN and GaN. Particle size values gained from UDM, USDM and UDEDM are very near to each other. Strain values are found the same in all three methods. For InGaN layer, it first increases and later decreases, for AlGaN layer it decreases and for GaN layer it increases with an increase in temperature. Uniform stress values presented the same behavior as the strain for each three layers. Anisotropic energy density values showed decreasing later increasing behavior for InGaN, continuously decreasing for AlGaN, and increasing for GaN layers with an increase in temperature. The increase in anisotropic energy density for InGaN and GaN, and the decrease in AlGaN is due to the increase of the stress values along with the temperature.

On the other hand according to Scherrer method for InGaN layer in sample A, results gained for  $\sin\theta$  are 0.5% smaller than for  $\cos\theta$ . The same comparison is 15% for sample B and 11% for sample C. In GaN layer similar behaviors are noticed as InGaN. For InGaN layer values are three or four times larger than the others. This

increase in values is proportional with growth temperature. Broadening of lines in HR-XRD is thought to be caused from particle size and lattice strain. All the results gained in this study are in good agreement with ones in literature. Especially, it is noticed that UDEDM method is the most suitable method for calculating strain and other parameters.

**Acknowledgements** This work was supported by the Presidency Strategy and Budget Directorate (Grants Number 2016K121220).

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