

## ANALYSIS OF THE 2D NONCONCENTRIC LARGE REFLECTOR ANTENNA-IN-RADOME SYSTEM: H-POLARIZATION CASE

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**Abstract** – 2D nonconcentric reflector antenna-in-radome system is analyzed for H-polarization case. Rigorous formulation is performed depending on the MoR, Green's function and CSP methods. Larger geometries are solved in reasonable cpu times by using the FFT based algorithm in the computation of the Green's function.

### I. INTRODUCTION

The radome is coverage of the reflector antenna system, but it makes an effect on the radiation characteristics. Therefore it is necessary to have accurate simulation tools for the engineering design purposes.

The older ray tracing techniques were extended by considering the all hybrid ray combinations during the transmission through the radome [2]. Radome problems can also be solved by using numerical methods like the MoM or the FEM technique for the electrically small and medium size geometries.

The circularly cylindrical reflector antenna and the covering concentric circular radome was a problem of interest and it was analyzed in [4] for both polarization cases. The nonconcentric circular radome covering the circularly cylindrical reflector antenna system is another problem of interest and it was solved in [5] again by combining MoR, Green's function technique and CSP method. Furthermore in this study an optimization is performed depending on the problem parameters.

The present study can be considered as the different computational way of the previous work performed in [5]. In that study it was noted that a special care should be taken in the numerical evaluation of the successive summations. These summations come from the geometrical transformations of the cylindrical wave functions by the well-known addition theorem. However here due to the periodic nature of the problem one can expand green's function into the Fourier series on the radome centered coordinate system. Then the scattered part of the green's function can be easily computed in the other reflector centered coordinate system by using the available FFT algorithm. The FFT algorithm based formulations of the electromagnetic scattering problems were also used in literature related with the MoR techniques. This way of computation provide us to solve the larger problems in the more reasonable cpu time durations and no further efforts are spent on the convergence of the successive series.

### II. FORMULATION

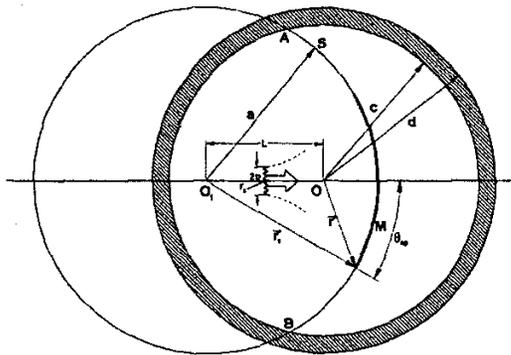


Fig. 1. Geometry of the problem.

Geometry of the reflector antenna and its covering radome system is given in Figure 1. Here there is a 2D circularly cylindrical pec reflector surface with radius "a" and its half angle is  $\theta_{ap}$ . It is covered by a circular dielectric radome which is characterized by the relative permittivity  $\epsilon_r$  and the relative permeability  $\mu_r$ . Also the inner and outer radius's of the radome are given as c and d respectively. The center of the radome is shifted from the center of the reflector by a distance L. The feed is assumed to be a complex point line source located on the axis of symmetry of reflector-in-radome system i.e.  $r_0$ . In addition the complex position of the line source provides us to determine the beam width and the beam direction of the incident field [1].

The requirements for the rigorous formulation of the presented problem can be stated as satisfying the 2-D Helmholtz wave equation, the Sommerfeld radiation condition at  $r \rightarrow \infty$ , the Meixner condition at the reflector edges, the Neumann boundary condition on the reflector surface M, and further the tangential components of the electric and magnetic field have to be continuous on the radome boundaries.

The following IE is obtained by imposing the Neumann boundary condition on the reflector surface M.

$$\int_M J_{\varphi_1}(\bar{r}_1') G_{\varphi_1}^E(\bar{r}_1, \bar{r}_1') d\bar{r}_1' = -\frac{\partial H_z^{in}(\bar{r}_1)}{\partial r_1}, \quad \bar{r}_1 \in M \quad (1)$$

where  $J_{\varphi_1}$  is the induced surface current density on the reflector M and  $G_{\varphi_1}^E$  is the Green's function of the circular dielectric shell i.e.  $G_{\varphi_1}^E = \frac{\partial^2 G^0}{\partial r_1 \partial r_1'} + G^{sc}$  where  $G^0$  is the free space scalar Green's function in 2D. Besides

$G^{sc}$  is the scattered part of the total Green's function of the circular shell which is given in [4] explicitly. One can consider the values of the  $G^{sc}$  on the closed circular contour C that is the combination of the reflector part M and its complementary part S. The expression of the  $G^{sc}$  in the  $(r_1, \varphi_1)$  coordinate system i.e. on C can be obtained by using the required geometrical transformation between two coordinate system.

$$G^{sc}(\varphi_1, \varphi_1') = \frac{-i}{4} \sum_{n=-\infty}^{\infty} K_n^e g(r_1 = a, \varphi_1) g^*(r_1' = a, \varphi_1') \quad a > L \quad (2)$$

Here the source and the observation points are taken on C and furthermore g function is defined as follows

$$g(r_1, \varphi_1) = \begin{cases} f(r_1, \varphi_1) & Q: -\varphi_m \leq \varphi_1 \leq \varphi_m \\ \frac{f(r_1, \varphi_m) - f(r_1, -\varphi_m)}{2\varphi_m} \varphi_1 + \frac{f(r_1, \varphi_m) + f(r_1, -\varphi_m)}{2} & (-\pi, \pi) / Q \end{cases} \quad (3)$$

where  $f(r_1, \varphi_1) = \frac{\partial(J_n(kr)e^{in\varphi})}{\partial r_1}$  and  $r = \sqrt{r_1^2 + L^2 - 2r_1L \cos \varphi_1}$ . Also  $\varphi$ (or  $\varphi'$ ) is the function of the  $\varphi_1$ (or  $\varphi_1'$ ) and the other geometry parameters.

In this way of the definition there is no need to use the all parts of  $G^{sc}$  for the 3 separate regions of the radome. Because it is seen that the only observation and source points on M are crucial in the solution of IE in (1). For the other external points on C it may be approximated by any suitable function and here it is chosen as the linear equation between the points A( $a, \varphi_m$ ) and B( $a, -\varphi_m$ ). The mentioned function  $G^{sc}(\varphi_1, \varphi_1')$  is expanded into the double Fourier series with respect to two arguments producing the coefficients  $h_{nm}$ . Furthermore it can be said that this definition of the  $G^{sc}$  on the circular contour C entail that the  $h_{nm}$  coefficients asymptotically decay as  $O(|n|^{-2-\epsilon} |m|^{-2-\epsilon})$ . Their efficient computation needs double integration of rapidly oscillating functions and here it is performed by the double FFT algorithm.

When the IE given in (1) is written in series form in DFT domain, the singular part i.e. static part can be analytically inverted by RHP technique. For this purpose a special canonical dual series can be used [3]. Then the formulation finally produces an algebraic matrix of Fredholm 2<sup>nd</sup> kind. So the existence, uniqueness and convergence can be guaranteed.

### III. NUMERICAL RESULTS

It is observed that the convergence criteria indicated in principle really satisfied and this is shown in Figure 2. Figure 3 presents the normalized radiation pattern for free space and in the presence of radome. It is also seen in this figure that half wavelength design really reduces the distortion in the pattern and it approaches to the free space pattern. Finally in Figure 4 the variation of the directivity and normalized total power with respect to the radome thickness is shown for various feed positions. For a specific  $r_0/a$  value, the directivity is increased more than the free space value if the thickness is taken as  $0.555\lambda_0$ . Although the absolute excess is almost same with the case given in [5], the relative increase in directivity is low for this larger case. The same figure also presents the

total power variation with the radome thickness and a small amount of increase is observed for the indicated specific radome thickness and feed position.

IV. CONCLUSION

For the accurate simulation of the small radomes, the previous solution [5] is tried to be improved. FFT techniques are used for the computation of the Green's function to perform this solution. Radiation characteristics are obtained for larger geometries in reasonable cpu times.

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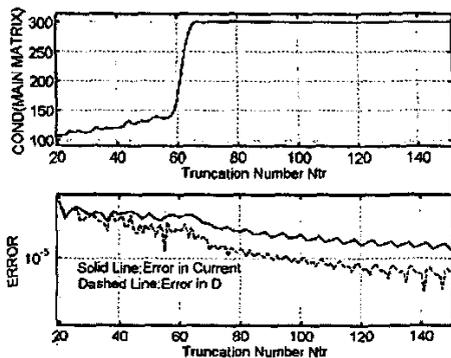


Fig. 2. (a) Condition number versus Ntr  
 (b) Error in directivity and current versus Ntr.

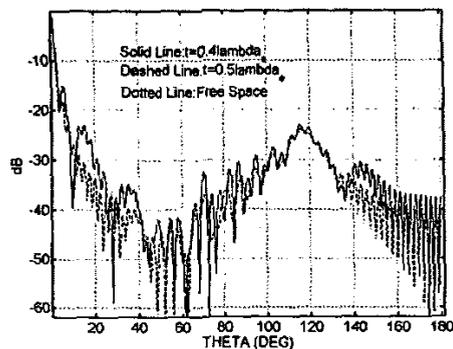


Fig. 3. Normalized Radiation pattern for a = 25λ, L = 19.9λ, c = 31.83λ, r/a = 0.5, θap = 30°, kb = 2.6 and εr = 2, μr = 1

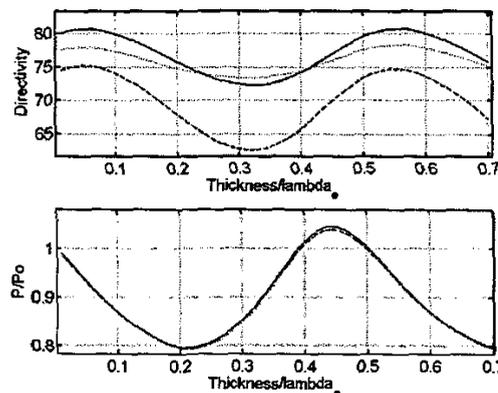


Fig. 4. Variation of the directivity and normalized total power versus radome thickness for various feed positions. a = 15 λ, L = 10 λ, c = 18 λ, θap = 30°, εr = 2, μr = 1, kb = 2.6, β = 0° and Ntr = 190. Solid curve is the r/a = 0.526 (optimized one), Dashed curve is the r/a = 0.55 and Dotted curve is the r/a = 0.51. Free space directivity 79.51 for r/a = 0.526.