Effects of task format on probabilistic forecasting of stock prices

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Abstract

This study aims to explore the differences in various dimensions of forecasting accuracy that may result from the task format used to elicit the probabilistic forecasts. In particular, we examine the effects of using multiple-interval and dichotomous formats on the performance of portfolio managers' probabilistic forecasts of stock prices. Probabilistic forecasts of these experts are compared with those provided by semi-experts comprised of other banking professionals trained in portfolio management, as well as with forecasts provided by a novice group. The results suggest that the task format used to elicit the probabilistic forecasts has a differential impact on the performance of experts, semi-experts, and novices. The implications of these findings for financial forecasting are discussed and directions for future research are given.

Keywords: Subjective probability; Probability forecasting; Judgmental forecasting; Stock-price forecasting; Task format

1. Introduction

The critical role of judgment in forecasting, especially in economic and financial forecasting, is emphasized unequivocally by research findings (Batchelor and Dua, 1990; Bunn and Wright, 1991; Flores et al., 1992; Goodwin and Wright, 1991; McNees, 1990; Phillips, 1987; Turner, 1990; Wolfe and Flores, 1990; Wright and Ayton, 1987; Zarnowitz and Lambros, 1987). The question remains as to how to structure and integrate such expert judgment into financial decision-making processes. The use of subjective probabilities as ways of reflecting the uncertainty inherent in financial forecasting situations (as well as the forecaster's internal state of uncertainty) provides one promising answer. Probability forecasts supply efficient channels of communication between the providers and users of financial information, since they offer quantitative measures of such uncertainty.

In stock-price forecasting, subjective probability distributions were first used by Bartos (1969) and Stael von Holstein (1972). In both studies, uniform distributions outperformed the forecasters' distributions. In later studies (Yates et al., 1991; Önal and Muradoğlu, 1994), probabilistic forecasts of stock prices were again found to display low levels of accuracy. Furthermore, historical forecasters (relying on relative frequencies) were found to outperform the probabilistic forecasts given by the participants. Yates
et al. (1991) attributed this observed difficulty in stock-price forecasting in part to the efficiency of the market. In an efficient market, stock prices (which are known to everyone operating in the market) represent all the available information. Therefore, it is not possible to systematically make better forecasts of future prices, leading to consistently abnormal profits (Fama, 1991).

Yates et al. (1991) also identified the presence of an 'inverse-expertise effect' in forecasting performance. This effect was defined as the existence of a negative relationship between forecasting accuracy and expertise. Replicating their study, Önkal and Muradoğlu (1994) changed the environmental set-up to an emerging and inefficient stock market. However, the inverse-expertise effect persisted.

There were two main limitations of this research. First, both studies only used multiple-interval task formats. It may be argued that the choice of task formats could directly influence various aspects of probability judgment accuracy (Ronis and Yates, 1987), therefore requiring detailed investigation. Second, both studies used students as forecasters. Yates et al. (1991) identified graduate students as experts, while Önkal and Muradoğlu (1994) defined experts as students who have made previous stock investment decisions.

The purpose of this study was to explore the effects of using different task formats (i.e. multiple-interval and dichotomous formats) on the performance of portfolio managers' probabilistic forecasts of stock prices. Obtaining differential performances under different task formats would have important policy implications for training, evaluation, and user satisfaction in financial forecasting settings. The particular task formats used in this study were selected on the basis of the needs and expectations of the users of such financial forecasts.

Probability forecasts given by portfolio managers (i.e. the 'expert' group) were also compared with those provided by a 'semi-expert' group comprised of other banking professionals trained in portfolio management, as well as a 'novice' group. The design allows us to explore the inverse-expertise effect across different task formats and to generalize the research to non-student subjects. Following Önkal and Muradoğlu (1994), forecasting is studied in a developing economy setting of an inefficient emerging security market so as to deter misinterpretations of forecast accuracy via market efficiency assumptions (i.e. so as to avoid arguments relating the difficulty in forecasting stock prices to the notion of efficient markets where consistently better abnormal profits are not attainable).

2. The setting: An emerging securities market

Financial markets in Turkey were highly inefficient and strictly regulated until 1980. Attempts to liberalize the country in general and financial markets in particular started at the beginning of the 1980s with the introduction of a liberalization package encouraged by the World Bank and the International Monetary Fund. Establishment of the legal framework and regulatory agencies for the stock market were completed in 1982, but it was only in 1986 that the Istanbul Securities Exchange (ISE), the only stock exchange in Turkey, was established. During the first two years of its operations, the employees of the stock exchange could hold stock portfolios without notification and there was no legislation against insider trading until 1990. During February 1992, when this study was conducted, 143 stocks were traded at ISE and the average daily volume of trade was US$55 million. There were 162 intermediaries and brokerage houses, 60 of which were affiliated with companies traded in the exchange.

The relatively few stocks and the low volume of trade in ISE compared with exchanges in developed countries decreases the complexity of the decision parameters and of the forecasting task. Also, the market is inefficient in the weak and semi-strong forms. That is, the stock prices are found to be forecastable based on past price performance (Muradoğlu and Unal, 1994), and based on macroeconomic variables (Muradoğlu and Önkal, 1992). Owing to market size and institutional inefficiencies, professional portfolio
managers can be assumed to have access to private information.

3. Procedure

Participants in the study were reached at two locations on the same date. The first group (referred to as ‘experts’) was composed of portfolio managers. This group consisted of 13 experts working for a bank-affiliated brokerage house. All the experts had licenses as brokers and their job descriptions included management of four investment funds and the provision of investment advice to customers with investments above US$50,000. The second group (referred to as ‘semi-experts’) was composed of experts working for the banking sector as internal auditors and managers. They were participating in a company-paid 40-hour workshop on portfolio management. Of this group, two internal auditors and seven managers were willing to participate in the experiment after the completion of the workshop.

To enhance the generalizability of the findings, the experiment was also replicated with a sample of 64 students from the Faculty of Business Administration at Bilkent University. This sample was used as the ‘novice’ group.

Following the basic procedure of Yates et al. (1991), the task involved preparing probability forecasts regarding the closing stock prices of 32 companies listed on the Istanbul Stock Exchange. The companies with the highest volume of trade during the preceding 52-week period were selected to minimize task complexity. This selection was made to ensure that the relevant stock prices could easily be followed by all participants.

The choice of task formats employed in this study was based on interviews with potential users of financial forecasts. In response to the needs and expectations of users, multiple interval and dichotomous task structures were selected as alternative formats that forecasters could utilize to express their true judgments. Accordingly, subjects were asked to make forecasts regarding the weekly price changes for each of the 32 stocks using (1) a multiple interval format, and (2) a dichotomous format. Forecasts were made regarding the percentage change between the previous Friday’s closing stock price and the closing stock price that would be realized the current Friday. In the multiple-interval format, subjects provided these forecasts in the form of subjective probabilities conveying their degree of belief in the actual price change falling into the designated percentage change categories. Specifically, subjects were asked to complete a response form (Fig. 1) for each stock.

The range of stock price changes in the response form were prepared by considering the average weekly changes in the composite stock index of ISE during the previous 52-week period. For the previous 52 weeks, weekly price changes were 3% on average with a maximum increase of 8% and a maximum decrease of 5%. The first 5% increase range (Interval 5) contained the average weekly increase during the previous year, the second (Interval 6) contained the maximum weekly increase observed in the previous 52-week period. Intervals 7 and 8 were designed for stocks whose volatility is higher than average. Intervals 1–4 were chosen as symmetric to Intervals 5–8.

Forecasts with the dichotomous format involved stating whether the forecaster believed the closing stock price for the current Friday would (a) increase, or (b) decrease or stay the same in comparison with the previous Friday’s closing stock price. Subjects were then requested to convey their degree of belief with a subjective probability for the forecasted direction of price change. Specifically, subjects were asked to complete a response form (Fig. 2) for each stock.

At the beginning of the experiment, particip-

\[
\begin{array}{c|c|c}
\text{WEIGHT PRICE CHANGE INTERVAL} & \text{PROBABILITY} \\
(\text{in percentages, Friday to Friday)} & \\
(0) & \text{INCREASE 15% or more} & \_ \_ \% \\
(7) & \text{INCREASE 10% - up to 15%} & \_ \_ \% \\
(6) & \text{INCREASE 5% - up to 10%} & \_ \_ \% \\
(5) & \text{INCREASE up to 5%} & \_ \_ \% \\
(4) & \text{DECREASE 0% - up to 5%} & \_ \_ \% \\
(3) & \text{DECREASE 5% - up to 10%} & \_ \_ \% \\
(2) & \text{DECREASE 10% - up to 15%} & \_ \_ \% \\
(1) & \text{DECREASE 15% or more} & \_ \_ \% \\
\hline
& \_ \_ \% \\
\end{array}
\]

Fig. 1. Form 1.
When compared to the previous Friday's closing price, this Friday's closing price will
A. Increase
B. Stay the same or decrease

Your forecast (A or B): ____________

Probability that your forecast will indeed occur (i.e., probability that the weekly price change will actually fall in the direction you predicted) (between 0 and 100%): ____________

Fig. 2. Form 2.

Participants were given detailed definitions of 'subjective probability' and 'probability forecasting tasks'. Examples were discussed and the design of the study was described. Participants were also informed about the research goals. The findings of previous research regarding the inverse-expertise effect were not discussed with the subjects so as not to influence their motivation.

Participants were told that certain scores of probability forecasting performance would be computed from their individual forecasts. They were informed that, owing to the computational characteristics of these scores (i.e. proper scoring rules), each subject could earn the best potential score by expressing his/her true opinion without hedging or bluffing. Subjects were also told that their performance would be reported on a personal basis and no information about their direct or implied individual performances would be given to their managers or co-workers.

Each participant was presented with a folder that contained background forms and response sheets for the 32 companies in question. Background forms contained information on the name of the company, its industry, its net profits as of the end of the third quarter of 1991, earnings per share, and price-earnings ratio as of the last day of the preceding week. The folders also provided the weekly closing stock prices (i.e. the closing stock prices for each Friday) of the preceding 3 months (12 weeks) in tabular form as well as the weekly closing prices for the last 52 weeks in graphic form.

Response sheets were comprised of the two formats illustrated previously for each company (i.e. one being the response form containing the previously-illustrated multiple interval format and the second being the response form containing the previously-illustrated dichotomous format). Both response sheets also contained instructions about the forecasting task.

Participants were allowed to take the background folders home. They were given the experimental material on Friday afternoon and were requested to submit the completed response sheets by Monday 9 a.m. before the opening of the session at the stock exchange. They were also permitted to utilize any information source they would like in making their forecasts, excluding the other participants of the study. This was facilitated by the fact that the forecasts were made over the weekend when the expert and semi-expert groups would not meet at their natural job settings.

4. Findings

Performance measures used to evaluate the various aspects of forecasting accuracy of multiple-interval forecasts were the mean probability score for multiple events, calibration score, scatter score, mean slope, forecast profile variance, and the skill score. The mean probability score provides an index of overall forecasting accuracy. Calibration indexes the forecaster's ability to match the probability forecasts with the realized relative frequencies. Scatter gives a measure of excessive variability in the forecasts. The mean slope reflects the forecaster's ability to discriminate between occasions when the actual price change will and will not fall into the specified intervals. The forecast profile variance compares the forecaster's probability profile with a flat profile that shows no variability across intervals (as would be given by a uniform forecaster). Finally, the skill score conveys the total effect of those mean probability score components that are mainly under the forecaster's control, hence reflecting the global forecasting skill. (For details of these components, see Appendix A.)

Pairwise comparisons of performances of experts, semi-experts, and novices were made on each of the performance measures via Mann–Whitney U tests. The performances of these groups were also compared with those of the
uniform and historical forecasters using sign tests. The uniform forecaster gives equal probabilities to all intervals, and hence provides a no-knowledge performance standard. A limited-knowledge performance standard is given by a historical forecaster who relies exclusively on past values. We employed two distinct definitions for historical forecasters. According to the first definition (H1), a historical forecaster is one who assigns probabilities to intervals that are equivalent to the last week’s realized relative frequencies (which are constant for all the stocks, as in Yates et al., 1991). According to the second definition (H2), a historical forecaster is one who gives probabilistic forecasts for each stock that are equal to the last week’s realized outcome vector (with a probability of 1.0 for the realized interval and 0 for the remaining intervals) for that stock. The first definition enables comparisons of the forecasters’ performances with a market-wide historically-based distribution; whereas the second definition permits comparisons of forecasters’ performances with stock-specific historically-based distributions.

Table 1 displays the median values of the performance measures for the multiple-interval forecasts of experts, semi-experts, novices, the uniform forecaster, and the two historical forecasters. Experts showed pronounced differences in slope and skill scores ($p = 0.024$ and $p = 0.026$, respectively, for comparisons with semi-experts; $p = 0.023$ and $p = 0.021$, respectively, for comparisons with novices). No significant differences were found between semi-experts and novices on any of the measures. Kruskal-Wallis tests also indicated that the only significant differences among the three groups were found for the slope ($p = 0.006$) and the skill ($p = 0.012$) components. The better mean slopes of experts (in comparison with both semi-experts and novices) indicate that experts were better in discriminating between instances when the actual price change would and would not fall into the specified intervals. The better skill scores of the experts demonstrate that the overall effect of those PSM components under the forecasters’ control was more pronounced for the experts when compared with both the semi-expert and the novice groups.

The experts’ performances, however, were not found to surpass the uniform forecaster. Only 38.5% of experts attained PSM scores better (i.e. lower) than the PSM of the uniform forecaster, representing no significant differences ($p > 0.10$). It is worth noting here that the performance of the uniform forecaster depends on the number of categories that are used in the multiple-interval format.

Using last week’s market-wide relative frequencies as forecasts for the current week, the first historical forecaster (H1) performed better than the experts on all measures ($p = 0.0001$ for

<table>
<thead>
<tr>
<th>Performance measure</th>
<th>Experts</th>
<th>Semi-experts</th>
<th>Novices</th>
<th>U</th>
<th>H1</th>
<th>H2</th>
</tr>
</thead>
<tbody>
<tr>
<td>PSM↓</td>
<td>0.937</td>
<td>1.051</td>
<td>1.040</td>
<td>0.875</td>
<td>0.771</td>
<td>1.250</td>
</tr>
<tr>
<td>Calibration↓</td>
<td>0.171</td>
<td>0.210</td>
<td>0.183</td>
<td>0.123</td>
<td>0.019</td>
<td>0.020</td>
</tr>
<tr>
<td>Scatter↓</td>
<td>0.058</td>
<td>0.105</td>
<td>0.101</td>
<td>0.000</td>
<td>0.000</td>
<td>0.738</td>
</tr>
<tr>
<td>Mean slope↑</td>
<td>-0.015*$^*$</td>
<td>-0.045</td>
<td>-0.040</td>
<td>0.000</td>
<td>0.000</td>
<td>0.106</td>
</tr>
<tr>
<td>F. profile variance</td>
<td>0.038</td>
<td>0.031</td>
<td>0.029</td>
<td>0.000</td>
<td>0.011</td>
<td>0.109</td>
</tr>
<tr>
<td>Skill↓</td>
<td>0.185*$^*$</td>
<td>0.319</td>
<td>0.308</td>
<td>0.123</td>
<td>0.109</td>
<td>0.498</td>
</tr>
</tbody>
</table>

$^*$: Smaller values better; $↑$: larger values better.
No direction given for F. profile variance since it compares forecaster’s probability profile with a uniform profile.
$^*$ Better than semi-experts.
$^*$ Better than novices.
$^*$ $p < 0.05$. 

No direction given for F. profile variance since it compares forecaster’s probability profile with a uniform profile.
$^*$ Better than semi-experts.
$^*$ Better than novices.
$^*$ $p < 0.05$. 


PSM, scatter and skill; $p = 0.002$ for calibration; $p = 0.046$ for mean slope). Using last week's realized (stock-specific) outcome vectors for each stock, the second historical forecaster (H2) performed generally worse than the experts. In fact, 92.3% of experts attained better PSM scores than H2 ($p = 0.002$). The superior performance of experts was mainly due to the better scatter (100% obtained better scores than H2; $p = 0.0001$), and skill scores (92.3% obtained better scores than H2; $p = 0.002$). These findings can perhaps be interpreted with an argument for H2 providing a stock-specific performance threshold for experts, who are expected to forecast stock prices on the basis of the properties of individual stocks rather than market movements (as is the case with H1). It may be argued that the experts’ forecasts incorporate rational expectations (i.e. expectations about the future stock prices) whereas the historically-based forecasts are built on the past performances of stock prices which represent adaptive expectations. These findings may also be related to the definition of H2 as a short-sighted stock-specific historical forecaster, who only considers the individual performance of stocks of the previous week. It may be argued that, depending on market conditions, a more realistic stock-specific performance standard would have a longer memory horizon. Such a performance standard would primarily be concerned with the formation of adaptive expectations, an area definitely worth pursuing as an extension of current research.

In order to be able to compare multiple-interval forecasts with dichotomous forecasts, multiple-interval forecasts were sign-aggregated (i.e. dichotomized) by the researchers. That is, the probabilities assigned to Intervals 5–8 on the multiple-interval format were summed and used as the probability assigned to the stock price increasing. Likewise, probabilities assigned to Intervals 1–4 on the multiple-interval format were summed and used as the probability assigned to the stock price decreasing or staying the same. The resulting sign-aggregated forecasts were then comparable with dichotomous forecasts.

Performance measures used to evaluate various dimensions of forecasting accuracy of dichotomous and sign-aggregated forecasts were the mean probability score ($\bar{PS}$), scatter, slope, calibration, and bias scores (for details on these measures, see Appendix B). If the outcome index is defined in terms of stock price increases, $\bar{PS}$ gives a measure of overall accuracy, and scatter presents the excessive variability in forecasts. Slope provides an indication of the forecaster’s success in separating cases where the stock price will and will not increase. Calibration (referred to as ‘price-increase calibration’) measures the extent to which the probabilistic forecasts match the relative frequencies of occurrence of stock price increase. Bias (referred to as ‘over/underforecasting’) gives an indication of the tendency to judge the stock price increase as being more likely (overforecasting) or less likely (underforecasting) than it really is. Positive bias scores reflect overforecasting (i.e. the mean probability assigned exceeding the relative frequency of price increase), and negative bias scores reflect underforecasting (i.e. relative frequency of price increase exceeding the mean probability assigned).

The outcome index may also be defined in terms of the correctness of the forecaster’s predicted outcome. In this case, $\bar{PS}$ and scatter have similar interpretations, while slope gives an indication of the forecaster’s ability to distinguish when (s)he is correct from when (s)he is incorrect. Calibration (referred to as ‘predicted-outcome calibration’) provides an index of how closely the probabilistic forecasts match the proportions correct. Bias (referred to as ‘over/underconfidence’) reflects the forecaster’s tendency to judge the actual occurrence of the predicted outcome as being more likely (overconfidence) or less likely (underconfidence) than it really is. Positive bias scores reflect overconfidence (i.e. the mean probability assigned exceeding overall proportion correct), and negative bias scores reflect underconfidence (i.e. overall proportion correct exceeding the mean probability assigned).

The performance measures that are reported include $\bar{PS}$, scatter, slope, price-increase calibration, over/underforecasting, predicted-out-
come calibration, and over/underconfidence. Scatter and slope scores were only given for the first outcome-index definition, since both definitions yield similar results and the first definition may be viewed as providing a direct comparison with the multiple-interval case. Naturally, $PS$ scores were identical under the two definitions.

Performances of experts, semi-experts, and novices were compared pairwise using Mann–Whitney $U$ tests for each of the performance measures. Wilcoxon signed-ranks tests were used to compare the performances of the dichotomous and the sign-aggregated forecasts for each of the groups. Sign tests were employed to compare the performances of these groups with the uniform and the two historical forecasters.

Table 2 displays the median values of the performance measures for the dichotomous and the sign-aggregated forecasts of experts, semi-experts, and novices. It can be observed from this exhibit that dichotomous forecasts given by experts and semi-experts were essentially the same. However, both experts and semi-experts attained better $PS$ and over/underconfidence scores than novices ($p = 0.0001$ and $p = 0.006$ for $PS$ comparisons of novices with experts and semi-experts, respectively; $p = 0.0001$ and $p = 0.048$ for over/underconfidence comparisons of novices with experts and semi-experts, respectively). Also, experts’ discrimination was better than novices, as displayed via slope scores ($p = 0.0001$). For price-increase calibration and over/underforecasting, novices outperformed both the experts and the semi-experts ($p = 0.014$ and $p = 0.005$ for price-increase calibration comparisons of novices with experts and semi-experts, respectively; $p = 0.0000$ for over/underconfidence comparisons of novices with both the experts and the semi-experts).

An analysis of the sign-aggregated forecasts showed that, when the probability forecasts provided using multiple-interval format were condensed into dichotomous format, experts generally outperformed both the semi-experts and the novices. In particular, when compared with semi-experts, experts showed a superior overall accuracy (as indexed by the mean probability score; $p = 0.007$), accompanied by lower

<table>
<thead>
<tr>
<th>Performance measure</th>
<th>Dichotomous forecasts</th>
<th>Sign-aggregated forecasts</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Experts</td>
<td>Semi-experts</td>
</tr>
<tr>
<td>$PS$</td>
<td>$0.205^{***N}$</td>
<td>$0.221^{**N}$</td>
</tr>
<tr>
<td>Scatter</td>
<td>$0.030$</td>
<td>$0.036$</td>
</tr>
<tr>
<td>Slope</td>
<td>$0.119^{***N}$</td>
<td>$0.059$</td>
</tr>
<tr>
<td>Price-increase calibration</td>
<td>$0.187$</td>
<td>$0.194$</td>
</tr>
<tr>
<td>Over/under forecasting</td>
<td>$0.370$</td>
<td>$0.411$</td>
</tr>
<tr>
<td>Predicted-outcome calibration</td>
<td>$0.085$</td>
<td>$0.074$</td>
</tr>
<tr>
<td>Over/under confidence</td>
<td>$-0.044^{***}$</td>
<td>$0.100^{N}$</td>
</tr>
</tbody>
</table>

$a$: Smaller values better; $b$: larger values better; $0$ = values near $0$ better.

$^*$ Better than experts.

$^*$ Better than semi-experts.

$^*$ Better than novices.

$p < 0.05$.

** $p < 0.01$.

*** $p < 0.001$. 
scatter \((p = 0.038)\), higher slope \((p = 0.024)\), better price-increase calibration \((p = 0.013)\), lower overforecasting \((p = 0.038)\), better predicted-outcome calibration \((p = 0.017)\), and lower overconfidence (as shown by a lower positive bias score; \(p = 0.038\)). When compared with the novice group, experts attained better scores in \(\bar{PS}\) \((p = 0.0000)\), scatter \((p = 0.014)\), slope \((p = 0.013)\), predicted-outcome calibration \((p = 0.0001)\), and overconfidence \((p = 0.0009)\). On the other hand, novices were found to do less overforecasting than both the experts \((p = 0.003)\) and the semi-experts \((p = 0.0000)\); also showing better price-increase calibration than the semi-experts \((p = 0.009)\).

Comparisons with the uniform forecaster demonstrated the superior performance of experts with respect to overall accuracy, especially in the sign-aggregated case. While only 69.2\% of experts performed better than the uniform forecaster when presenting forecasts using the dichotomous format \((p > 0.10)\), 84.6\% of experts performed better than the uniform forecaster in the sign-aggregated case \((p = 0.012)\). Given the previous findings on forecasters’ poorer performances in comparison with the uniform judge (Stael von Holstein, 1972; Yates et al., 1991), our results may reflect that the experts’ forecasting accuracy can in fact exceed that of a uniform forecaster especially when the forecasts elicited using a multiple-interval format are condensed into a sign-aggregated format.

Comparisons with a historical forecaster who uses last week’s realized relative frequencies for the market (i.e. H1) showed that the historical forecaster performed better in \(\bar{PS}\), scatter, price-increase calibration, overforecasting, and predicted-outcome calibration \((p = 0.0001 \text{ for all measures) for the dichotomous forecasts; and performed better only in scatter \((p = 0.002)\) for the sign-aggregated forecasts. This historical forecaster also attained poorer slope scores than the experts \((p = 0.046)\) in the dichotomous case. Comparisons with a historical forecaster who uses last week’s stock-specific outcome vectors as forecasts (i.e. H2) revealed a similar situation. Such a historical forecaster was found to perform better than experts in \(\bar{PS}\) \((p = 0.012)\), price-increase calibration \((p = 0.011)\), overforecasting \((p = 0.002)\), and predicted-outcome calibration \((p = 0.002)\) for the dichotomous forecasts only. This historical forecaster showed inferior scatter \((p = 0.011)\), slope \((p = 0.0001)\), and overconfidence \((p = 0.046)\) scores than the expert group in the dichotomous case; receiving poorer scatter \((p = 0.046)\), slope \((p = 0.002)\), and overconfidence \((p = 0.046)\) scores in the sign-aggregated case. These findings may be viewed as providing additional evidence that the sign-aggregation of multiple-interval forecasts leads to better expert performance.

A comparison of the dichotomous forecasts with the sign-aggregated ones revealed interesting results. Experts attained better \(\bar{PS}\) \((p = 0.020)\), price-increase calibration \((p = 0.017)\), overforecasting \((p = 0.002)\), predicted-outcome calibration \((p = 0.014)\), and overconfidence \((p = 0.002)\) scores when their forecasts were sign-aggregated. These findings indicated that, when the experts’ multiple-interval forecasts were condensed into the dichotomous scale, the resulting representation became better calibrated showing less overforecasting, and displayed better overall accuracy. Over/underconfidence scores also revealed that, while the experts showed underconfidence in providing dichotomous forecasts, they became overconfident when their multiple-interval forecasts were sign-aggregated. It should be noted that the experts were relatively less overconfident in the sign-aggregated situation and more underconfident in the dichotomous case, so that their over/underconfidence (in absolute terms) was better in the sign-aggregated representation. The better bias of experts in expressing their forecasts may be attributed to their initial use of the multiple-interval scale. Given that the experts are argued to employ richer representations (Murphy and Wright, 1984), the multiple-interval scale may be viewed as a more suitable format for expressing their beliefs, leading to an improved bias performance when such assessments are sign-aggregated in comparison with the direct elicitation of dichotomous assessments.

In contrast to the experts, the use of the dichotomous format led to better forecasts when
compared with the sign-aggregated format for both the semi-expert and the novice groups. In particular, semi-experts’ dichotomous forecasts showed better PS ($p = 0.033$), scatter ($p = 0.033$), slope ($p = 0.006$), price-increase calibration ($p = 0.033$), and over/underconfidence ($p = 0.005$) scores; while the novices’ dichotomous forecasts demonstrated better PS ($p = 0.014$), scatter ($p = 0.012$), price-increase calibration ($p = 0.003$), and predicted-outcome calibration ($p = 0.005$) scores. These findings also support Murphy and Wright’s (1984) argument that rich representations are a function of the level of expertise. Accordingly, the dichotomous scale may be viewed as providing a preferable medium of representation for expressing forecasts based on the limited knowledge domains of semi-experts and novices.

5. Conclusion

Elicitation of probabilistic forecasts from portfolio managers and other banking professionals participating in a portfolio management workshop provided the focus of this study. As noted by Bolger and Wright (1994), "...assessment of the quality of expert judgment is becoming a central issue for both researchers and practitioners" (p. 21). Focusing on the financial forecasting domain, this paper attempted to assess the probabilistic forecasting performances of experts (relative to the performances of semi-experts and novices) under different task formats.

The inverse-expertise effect suggested by studies employing mainly student subjects has not been confirmed in general in this study, which involved non-student participants as well. The results obtained for the multiple-interval, dichotomous, and the sign-aggregated situations did not reveal an inverse-expertise effect in probabilistic forecasts of stock prices, with the exception of price-increase calibration and over/underforecasting measures. The one-week forecast horizon employed in this study provides a plausible explanation for the lack of this effect across the different task formats utilized. Previous research has suggested that the inverse-expertise effect may be contingent upon the selected forecast horizon (Muradoğlu and Önkal, 1994). In particular, it has been found that the performance of experts becomes worse than semi-experts as the forecast horizon is extended, even though the experts perform significantly better than the semi-experts for shorter forecast horizons (Muradoğlu and Önkal, 1994). It may be argued that the shorter forecast horizons (e.g., one week) describe experts’ natural environments better in the sense that portfolio managers essentially make short-term forecasts in emerging markets with higher volatilities. The portfolio managers’ superior forecasting performance for the one-week horizon may in turn be attributed to the issue of ecological validity.

The alleged inverse-expertise effect has only been observed with price-increase calibration and over/underforecasting. In particular, the novices were found to display superior calibration in predicting price increases, as well as showing minimal over/underforecasting. Experts, on the other hand, were overforecasting, i.e. they had a higher tendency to judge a stock-price increase to be more likely than it really is. This finding confirms the results of previous studies examining brokerage analysts’ recommendations (i.e. buy/sell advice) (Pratt, 1993; Womack, 1995). It has been asserted that experts are biased for stock-price increases since they prefer to recommend a buy decision (reflecting an expected stock-price increase) rather than a sell decision (reflecting an expected stock-price decrease). The experts’ tendencies towards buy recommendations are viewed as stemming from the costs attached to incorrect judgments on sell recommendations (Pratt, 1993). These costs may include damage to the firm’s and the analysts’ reputation in terms of present and potential investment banking relationships and information flows. Therefore, sell recommendations are less frequent, and hence more visible and more risky (Womack, 1995). The resulting tendency of experts to make buy recommendations (indicating predicted stock price increases) was displayed in this study via significant overforecasting on behalf of the portfolio managers.

Experts’ sign-aggregated forecasts were better
than their dichotomous forecasts, while the reverse was true for semi-experts and novices. These findings may be viewed as suggesting that experts express their true predictions better when confronted with a multiple-interval format in comparison with a dichotomous format. In particular, the results imply that, while the experts can effectively utilize the more detailed format provided with the multiple-interval scale, semi-experts and novices perform better with the summarized/compact format presented with the dichotomous scale. These findings lend further support to previous research showing that response mode and the particular ‘framing’ of outcomes are significant factors in the elicitation of judgments (Tversky and Kahneman, 1982; Slovic et al., 1982). It may be argued that experts, who are endowed with abundant information, can potentially express this rich information better when presented with a response mode utilizing a wider scale (i.e. multiple-interval format) as opposed to a compressed scale (dichotomous format). On the other hand, the dichotomous scale may provide a better representation format for conveying forecasts based on the limited information sets of semi-experts and novices.

An aspect of forecasting accuracy that has received considerable research attention is the over/underconfidence component (Gigerenzer et al. 1991; Juslin, 1994; Keren, 1987; Lichtenstein et al., 1982; Paese and Sniezek, 1991). Our results confirmed the previous findings that expertise has significant effects on confidence (Wright et al., 1994; Trafimow and Sniezek, 1994). The superior performance of experts was especially pronounced when their multiple-interval forecasts were sign-aggregated, again emphasizing the use of a wider scale as a preferable representation format for expressing expert forecasts. The slight overconfidence displayed with the sign-aggregated assessments may indicate that the wider scale provided by the multiple-interval format might be encouraging the experts to assign higher probabilities to the predicted direction of a price change. A potential explanation may be that the experts have a tendency to start giving their forecasts by assigning probabilities to intervals addressing the predicted direction of a price change, which may in turn mean that they are left with lower probabilities for the remaining intervals. Another explanation could stem from the computational properties of the scores. Since the experts’ dichotomous judgments were slightly underconfident, some added positive bias would tend to make their PS scores better. On the other hand, the semi-experts’ and novices’ dichotomous judgments were slightly overconfident. Hence, any added positive bias in their multiple-interval judgments would tend to worsen their PS scores. Such possibilities need to be examined with detailed research on the cognitive processes underlying the experts’ probabilistic forecasts given under different task formats.

Multiple-interval forecasts of experts were found to outperform the historical forecasts based on stock-specific data in terms of overall accuracy, scatter and skill. When these forecasts were represented in sign-aggregated form, expert performance was observed to be superior in scatter, slope, and overconfidence. This indicates that the information regarding the expert’s uncertainty presents valuable financial information in the sense that it reflects rational expectations rather than adaptive expectations. Most financial forecasts are made under the assumption of adaptive expectations with the processing of past data via econometric techniques. Our findings may be viewed as suggesting that, given a pertinent task format, using probability forecasts that incorporate rational expectations of forecasters does not reduce the accuracy of forecasts, but on the contrary, presents enriched information (Glazer et al., 1990).

A fertile area of future research involves extensive comparisons of expert assessments with those given by historically-based forecasting techniques. For example, the performance of portfolios constructed using Markowitz’s efficient frontier that employs historically-based mean and variance estimates (Markowitz, 1959) can be compared with the performance of similar portfolios constructed via expert assessments (Bar- tos, 1969). Also, different benchmarks utilizing abnormal returns and/or models incorporating univariate time series can be used to compare
the accuracy of judgmental forecasts (for a
detailed discussion, see Brown, 1993). Such
future research will be particularly interesting in
the context of emerging and presumably ineffi-
cient markets, since the inaccuracies in forecasts
are less attributable to the characteristics of the
markets in such conditions.

Elicitation of experts' probabilistic forecasts
using multiple formats also demands future
work. Providing experts with information on
observed discrepancies in multiple elicitations,
incorporating self-checks on consistency and
coherence into the assessment processes, and
examining forecasters' revision processes remain
intriguing research areas. The role of feedback in
improving such elicitations of uncertainty also
awaits meticulous exploration (Benson and
Önal, 1992; Bolger and Wright, 1993, 1994;
Önal and Muradoğlu, 1995). Further research
investigating the effects of training and feedback
on the performance of experts' probabilistic
forecasts is required.

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Appendix A: Performance measures for
evaluating probabilistic forecasts expressed in
multiple-interval format

A.1. Mean probability score for multiple events

Let \( f = (f_1, \ldots, f_m) \) be the forecast vector given
by a forecaster for each of the stocks, with \( f_k \)
denoting a probability forecast that the stock's
price change will fall into interval \( k, k = 1, 2, \ldots, m \). Accordingly, let \( d = (d_1, \ldots, d_m) \)
deфине an outcome index vector, with \( d_k \) assuming
the value of 1 if the realized price change falls
within interval \( k \), and assuming the value of 0 if
it does not fall within interval \( k \). The probability
score for multiple events (\( PSM \)) can then be
defined as

\[
PSM = (f - d)(f - d)^T = \sum (f_k - d_k)^2.
\]

Hence, the mean of probability scores (\( \bar{PSM} \))
over a specified number of forecasting occasions
(i.e. over a given number of stocks) gives an
index of a forecaster's overall accuracy level.
The lower the score, better is the overall accura-
cy with respect to the stocks in question.
Components resulting from the Yates de-
composition of the \( PSM \) (Yates, 1988) are out-
lined next.

A.2. Calibration

Calibration provides information about the
forecaster's ability to match the probability as-
sessments with the realized relative frequencies.
For example, suppose that for a set of 100 stocks
a forecaster indicates that the price of each given
stock will increase up to 5%, and that the mean
of these probabilistic forecasts is 0.40. This
forecaster's 0.40 assessments are well calibrated
if an increase up to 5% is actually observed on
40 of the 100 stocks. Accordingly, a calibration
score is a function of \( f_k \) (mean probability fore-
cast for interval \( k \)), and \( d_k \) (realized relative
frequency for interval \( k \)). In particular,

\[
\text{calibration} = \sum (f_k - d_k)^2.
\]

Lower scores indicate better performance in
assigning appropriate probabilities to outcomes.

A.3. Scatter

Scatter is the remaining element of the overall
forecast variance that is not directly attributable
to the forecaster's ability to discriminate between
occasions when the actual price change will and
will not fall into the specified intervals. Given
that scatter is basically evidence of excessive
variance, lower values are more desirable. A
scatter index is computed as follows:

\[
\text{scatter} = \sum \text{scatter}_k = \sum \frac{1}{N} \left[(N_{1k} \cdot \text{Var}(f_{1k}))
+ (N_{0k} \cdot \text{Var}(f_{0k}))\right],
\]

where \( \text{Var}(f_{1k}) \) is the conditional variance of the
N_{1k} forecasts given for a price change falling into interval k when it actually occurred. Similarly, \( \text{Var}(f_{0k}) \) is the conditional variance of the \( N_{0k} \) forecasts given for a price change falling into interval k when it did not occur. As is clear, \( N = N_k = N_{1k} + N_{0k} \).

A.4. Mean slope

Mean slope addresses another performance aspect that exhibits the forecaster’s ability to discriminate between instances when the actual price change will and will not fall into the specified intervals. The higher the mean slope, the better the forecaster is able to discriminate. Mean slope is computed as follows:

\[
\text{mean slope} = \frac{1}{m} \sum_k \text{slope}_k
\]

\[
= \frac{1}{m} \sum_k (\bar{f}_{1k} - \bar{f}_{0k})
\]

where \( \bar{f}_{1k} \) is the mean of probability forecasts for a price change falling into interval k computed over all the cases where the realized price change actually fell into interval k. Similarly, \( \bar{f}_{0k} \) is the mean of probability forecasts for a price change falling into interval k computed over all the times when the realized price change did not fall into the specified interval. The number of intervals presented in the task is given by m, i.e. \( k = 1, 2, \ldots, m \).

A.5. Forecast profile variance

Forecast profile variance captures the discrepancy between a forecaster’s set of probabilities (i.e. \( f = (f_1, \ldots, f_m) \)) and a uniform set of probabilities (i.e. \( f = ((1/m), \ldots, (1/m)) \)). Accordingly, the forecast profile variance compares the forecaster’s probability profile with a flat profile displaying no variability across intervals. An index of the forecast profile variance could be computed as

\[
\text{forecast profile variance} = \frac{1}{N} \sum_k \left( \left( \frac{1}{m} \sum_k (f_k - (1/m))^2 \right) / m \right).
\]

This measure provides an opportunity to examine the profiles of probability forecasts from an ‘across-interval variance’ point of view. It presents an index of how different the forecaster’s probabilities are from those that would be given by a uniform forecaster.

A.6. Skill

The aggregate effect of those \( \overline{PSM} \) components under the forecaster’s control can be measured through a skill score, computed as

\[
\text{skill} = \overline{PSM} - \frac{1}{m} \sum \text{Var}(d_k) = \overline{PSM} - \frac{1}{m} \sum [(\bar{d}_k) \ast (1 - \bar{d}_k)]
\]

where \( \text{Var}(d_k) \) gives the variance of the outcome index \( d_k \) for the interval k. Given that \( d_k \) values are determined by the price changes realized in the stock market, \( \sum \text{Var}(d_k) \) reflects an uncontrollable element of \( \overline{PSM} \) (whose value is given by the conditions of the stock market). Removing this uncontrollable or ‘base-rate’ component from \( \overline{PSM} \), we are left with the overall effect of all those accuracy components that are mainly controllable by the forecaster. Noting that lower \( \overline{PSM} \) values reflect better accuracy levels, lower skill scores signal better overall forecasting quality.

Appendix B: Performance measures for evaluating probabilistic forecasts expressed in dichotomous format

When probabilistic forecasts are expressed in dichotomous format, there are two possible codings that could be utilized. The first coding (i.e. external coding) involves eliciting probabilistic forecasts for a given target event (e.g. stock price increase). These forecasts are then evaluated with the use of an outcome index that is defined with respect to the occurrence of the prespecified target event. The second coding (i.e. internal coding) requires that the forecaster first chooses one of two possible outcomes and then assesses the probability that his/her predicted outcome will indeed occur. An evaluation of these probabilistic forecasts is then made using an outcome index that is defined with respect to
the occurrence of the predicted outcome. As discussed extensively in Ronis and Yates (1987), although these codings share the same performance measures, their interpretations vary substantially. These measures and their connotation for the external and internal codings are discussed next. Since the computational formulas remain the same for both codings, they are only presented under the external coding discussion.

B.1. External coding

B.1.1. Mean probability score

A potential extension of the multiple-interval format to the dichotomous format involves defining $f_i$ as the probability forecast given for a target event (e.g. the probability that the stock price will increase). Accordingly, $0 \leq f_i \leq 1.0$. Letting the outcome index $d_i$ assume a value of 1 if the target event (i.e. price increase) indeed occurs for stock $i$, with $d_i$ assuming a value of 0 otherwise, the probability score for stock $i$ ($PS_i$) becomes

$$PS_i = (f_i - d_i)^2.$$ 

Hence, the mean of probability scores ($\bar{PS}$) over a specified number of forecasting occasions (i.e. over a given number of stocks) gives an index of a forecaster’s probability judgment accuracy. The lower the score, better is the overall accuracy with respect to the stocks in question.

Components resulting from the Yates decomposition of the $PS$ (Yates et al., 1989) are outlined next.

B.1.2. Calibration

Calibration provides information about the forecaster’s ability to match the probability assessments with the mean outcome indexes (i.e. relative frequencies of the occurrence of a price increase). The calibration component originated with the Sanders (1963) decomposition of $\overline{PS}$, and was further employed in the Murphy (1973) decomposition.

A forecaster is said to be perfectly calibrated if, for all the stocks to which (s)he has assigned a 0.1 probability, 10% of the stocks actually show a price increase; for all the stocks given a 0.2 probability, 20% actually increase in price, and so on. Accordingly, a calibration score can be computed as follows:

$$\text{calibration} = (1/N) \sum N_p (f_p - \overline{d}_p)^2,$$

where $f_p$ addresses the probability forecast categories (e.g. each forecast can be rounded to the nearest tenth, resulting in 0.0, 0.1, 0.2, ..., 1.0) which could be used by the forecasters. The total number of forecasts (i.e. stocks) is given by $N$, with $N_p$ representing the number of instances in which a forecast of $f_p$ is used. It follows that $\overline{d}_p$ shows the mean outcome index (i.e. the proportion of times the stock price actually increases) corresponding to forecast $f_p$. Lower calibration scores indicate better performance in assigning probabilities that match the relative frequencies of occurrence of a stock price increase.

B.1.3. Scatter

Scatter is an index of the useless variability in probabilistic forecasts, with lower values being more desirable. A scatter index is computed as follows:

$$\text{scatter} = \frac{\left((N_1 \cdot \text{Var}(f_1)) + (N_0 \cdot \text{Var}(f_0))\right)}{N},$$

where $\text{Var}(f_1)$ is the variance of probabilities for all the $N_1$ cases when the stock price increases, and $\text{Var}(f_0)$ is the variance of probabilities for the $N_0$ cases when the stock price does not increase. As is clear, $N = N_1 + N_0$.

B.1.4. Slope

Slope provides an indication of the forecaster’s performance in assigning higher probabilities to instances when the stock price actually increases versus those cases when it does not increase. The higher the slope, the better the forecaster is able to discriminate. Slope is computed as follows:

$$\text{slope} = (\bar{f}_1 - \bar{f}_0),$$

where $\bar{f}_1$ is the mean of probability forecasts for all the cases when the stock price increases, and $\bar{f}_0$ is the mean of probability forecasts for all the cases when the stock price does not increase.
B.1.5. Bias—over/underforecasting

Bias reflects the forecaster's performance in matching her mean probability assignments (\( \hat{f} \)) to the overall relative frequency of stock price increase (\( \hat{d} \)), that is,

\[ \text{bias} = \hat{f} - \hat{d}. \]

If the mean of the probabilistic forecasts exceeds the overall relative frequency of price increase, then the forecaster is said to be 'overforecasting'. On the other hand, 'underforecasting' is revealed when the overall relative frequency of the price increase surpasses the mean probability assignments.

B.2. Internal coding

B.2.1. Mean probability score

The dichotomous format may require the forecaster to first choose from two outcomes (i.e. whether the stock price will (a) increase, or (b) decrease or stay the same). Forecasters are then requested to convey their degrees of belief in the occurrence of the chosen outcome by assessing subjective probabilities associated with the forecasted direction of price change. Hence, \( f_i \) denotes the forecaster's probability that his/her chosen outcome will occur for stock \( i \). Accordingly, \( 0.5 \leq f_i \leq 1.0 \). Outcome index \( d_i \) assumes a value of 1 if the chosen outcome indeed occurs for stock \( i \), and takes on a value of 0 otherwise.

The mean of probability scores (\( PS \)) over a specified number of forecasting occasions (i.e. over a given number of stocks) gives an index of a forecaster's probability judgment accuracy. The lower the score, the better is the overall accuracy with respect to the stocks in question.

B.2.2. Calibration

Calibration provides information about the forecaster's ability to match the probability assessments with the mean outcome indexes (i.e. the proportion of correct forecasts). If a forecaster attains 50% correct forecasts for all her 0.5 assessments, attains 60% correct for all 0.6 assessments, etc. then the forecaster is said to be perfectly calibrated. Lower calibration scores indicate better performance in assigning probabilities that match the proportion correct.

B.2.3. Scatter

Scatter gives a weighted average of the variability in those instances when the predicted outcome actually occurs as well as the variability in those occasions when the predicted outcome does not occur. Hence, scatter is an index of the useless variability in probabilistic forecasts, with lower values being more desirable.

B.2.4. Slope

Slope provides an indication of the forecaster's performance in assigning higher probabilities to instances when her chosen outcome occurs than when it does not occur. The higher the slope, the better the forecaster is able to discriminate.

B.2.5. Bias—over/underconfidence

Bias reflects the forecaster's performance in matching her mean probability assignments (\( \hat{f} \)) to the overall proportion of correct forecasts (\( \hat{d} \)). If the mean of the probabilistic forecasts exceeds the overall proportion of correct forecasts, then the forecaster is said to be 'overconfident'. On the other hand, 'underconfidence' is revealed when the overall proportion correct surpasses the mean probability assignments (Lichtenstein and Fischhoff, 1977).

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