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Electrically controllable plasmon induced reflectance in hybrid metamaterials

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The tunable plasmon induced reflectance (PIR) effect has been numerically investigated and experimentally realized by hybrid metal-graphene metamaterials. The PIR effect is produced by two parallel strips of gold (Au) and controlled electrically by applying the gate voltage to the graphene layer. The PIR response is generated by the weak hybridization of two bright modes of the gold strips and tuned by changing the Fermi level (E_f) of the graphene. The total shift of 211.7 nm was achieved in the reflection peak by applying only 3 V. This concept of real time electrical tuning of PIR, with a modulation depth of ~49% and a spectral contrast ratio of 66.6%, can be used for designing optical switches, optical modulators, and tunable sensors. *Published by AIP Publishing*. https://doi.org/10.1063/1.5063461

Electromagnetically induced transparency (EIT) is a phenomenon that can be produced by quantum interference between the two excitation pathways of a laser-activated atomic medium.^{1,2} This can be used for slow light applications,³ optical storage,⁴ optical switching,⁵ biosensing applications,^{6,7} and quantum information processing.⁸ Recently, plasmon induced transparency (PIT), analogous to the EITeffect, has been investigated in different platforms. The PIT has been observed in metallic nanoparticles,^{9,10} metamaterial structures,^{11–13} plasmonic coupled nanocavities,¹⁴ hybrid plasmon waveguide systems,15 and integrated photonic structures.¹⁶ Among these, metamaterial based structures are the best option as they have been a powerful tool to control the interaction of light with matter.^{17–22} A variety of tuning mechanisms are possible to generate the tunable response of metamaterials, 23-26 which are electrical, 27-29 thermal, 30 or mechanical.³¹

To obtain PIT, the plasmonic mode can be either radiative (bright mode) or subradiant (dark mode).³² If the incident light couples directly, then it will produce bright modes that are spectrally broadened due to radiative damping. On the other hand, if the incident light is not coupled directly, it will generate dark modes that are weakly damped and spectrally narrow.³³ PIT has been realized by either the destructive interference of dark-bright modes¹¹ or detuning of the two bright modes.³⁴

Hybrid metamaterial based devices can generate a tunable PIT response that can be used for enhanced sensing and switchable camouflage systems.^{29,35–37} These devices operate in the transmission mode and require a transparent substrate that limits the design wavelengths based on the type of substrate being used.^{11–13,34} On the other hand, the light matter interaction of graphene on top of the reflecting surface is increased fourfold.³⁸ This enhanced local electric field on a reflecting surface in the presence of graphene can be used for better detection and modulation.^{39–42} Therefore, a plasmon induced reflectance (PIR) will be more promising and can be used for efficient optoelectronic devices. The PIR-effect has only been experimentally realized by Chun-Feng *et al.* in 2014.⁴³ The design is based on the cut-wire and split ring resonator acting as dark and bright modes, respectively. However, a dynamically tunable PIR design has not been investigated.

In this letter, we demonstrate a highly tunable PIR phenomenon with hybrid metal-graphene metamaterials. Our hybrid metamaterial based PIR device consists of a reflecting thin metallic film, a dielectric layer, and an electrically tunable hybrid metal-graphene structure, as shown in Fig. 1(a).



FIG. 1. Hybrid metamaterials for PIR. (a) 3D view of a PIR device with a schematic of the top gating. (b) The unit cell of a PIR device with two Au strips (golden).

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The two strips on top of the graphene layers will have their own plasmonic resonances, which can be controlled by the length of the strips, as shown in Fig. 1(b). The optical response of a PIR device can be engineered by two strips and the thickness of a dielectric layer. Moreover, this response can be broadly tunable by electrostatic doping. The optical properties of the graphene can be explained by the Pauli blocking principle.⁴⁴ Two types of band transitions are possible depending upon the energy of the incident photon. If the energy of the photon is less than $2E_{f}$, the intra-band transition is dominant. On the other hand, if the photon energy is higher than $2E_f$, the inter-band transition is dominant.^{45,46} The interplay of these transitions establishes the optical response of graphene. The intra-band transitions in the conduction or valence band give rise to a Drude-like response similar to noble metals, and inter-band transitions that are Pauli blocked give rise to a universal, flat absorption spectrum. The Drude response is typically observed for frequencies up to the far-infrared, whereas the flat absorption of 2.3% is observed at optical frequencies.⁴⁷

The surface conductivity of graphene can be modeled as an infinitesimally thin isotropic surface conductivity from both sides. The intra-band transition and inter-band transitions are presented in the following equations, respectively:⁴⁸

$$\sigma_{intra} = -j \frac{e^2 k_B T}{\pi \hbar^2 (\omega - 2j\Gamma)} \left[\frac{\mu_c}{k_B T} + 2ln \left(e^{\frac{-\mu_c}{k_B T}} + 1 \right) \right], \quad (1)$$

$$\sigma_{inter} = -j \frac{e^2}{4\pi\hbar} ln \left[\frac{2|\mu_c| - (\omega - 2j\Gamma)\hbar}{2|\mu_c| + (\omega - 2j\Gamma)\hbar} \right], \tag{2}$$

where *e* is the electron charge and k_B is the Boltzmann constant. Other parameters include the temperature (*T*), scattering rate (Γ), angular frequency (ω_c), and chemical potential (μ_c) which can be changed in numerical investigations.

Overall, graphene has three major advantages. First, being a 2D material, it enables device miniaturization down to the atomic length scale. Second, the doping level in monolayer graphene is highly tunable by applying a voltage to an electrical gate. Third, graphene exhibits an optical response ranging from terahertz to optical frequencies,⁴⁹ allowing for ultra-broadband operation. In particular, broadband optical modulators have been demonstrated.⁵⁰

We have numerically investigated a PIR device using the finite difference time-domain (FDTD) method using Lumerical FDTD Solutions. The unit cell of the design has two parallel Au strips. Both strips serve as two bright modes. Weak hybridization of these bright modes results in the PIReffect. The lengths of strips are selected as $0.8 \,\mu\text{m}$ and $1 \,\mu\text{m}$ and the width as W = 200 nm for both the strips, and the distance between two strips is kept as D = 200 nm. The periodic boundary condition is used for the x and y axes of the unit cell, and perfect matched layers (PMLs) are defined in the propagation direction. The design has a periodicity of 1.5 μ m in the x-axis and 1.0 μ m in the y-axis. A plane wave source along the z direction was used to illuminate the unit cell having the electric field component (E) parallel to the x-axis. For tuning the PIR response, four different values of E_f for graphene were investigated. By changing the E_f value which is equal to μ_c , the intra-band transition is changed, and the optical response of the overall device is tailored. The scattering rate (Γ) of graphene was set as 0.01 eV (2.4 × 10¹² s⁻¹), and the temperature (*T*) was set as 300 K.

The device fabrication is done by cleaning the Si substrate using oxygen plasma to remove the residue of the photoresist used for dicing. Al is deposited using an E-beam evaporator, and 50 nm of Al₂O₃ is deposited using atomic layer deposition (ALD). ALD is a technique in which a chemical reaction takes place on the surface to form a 1 nm thick oxide layer in each step. The process results in highly uniform thin films because of the slow rate. We have transferred graphene on top of the oxide layer with the wet transfer method. Poly (methyl methacrylate) (PMMA) A4 resist was spin coated and baked, and the sample was coated with a conductive polymer like aquaSAVE. The sample is exposed to E-beam lithography. After the exposure, the resist is developed using a solution of methyl isobutyl ketone (MIBK): isopropyl alcohol (IPA) (1:1). Once the sample is patterned, 5/50 nm Ti/Au was coated on patterned samples. Both metals were deposited using an E-beam evaporator. Structures were visible after the lift-off process in acetone for 24 h. The scanning electron microscopy (SEM) image of PIR structures is shown in the inset of Fig. 2(a).

In order to apply the gate voltage to graphene, BaF_2 substrates with the metal contacts at the corners were placed on top of the PIR device and separated by an insulating tape. An



FIG. 2. Simulated and FTIR measurement of PIR structures. (a) Simulated results for different E_f values. (b) Normalized reflection at -0.6 V, 0.4 V, 1.4 V, and 2.4 V. The total shift of the reflection peak and SEM image are presented in the inset.

ionic liquid is inserted between the two substrates, and a source was connected to the graphene layer and metal contacts using conductive tape. By applying the gate voltage, the capacitance is produced between the graphene layer and the gold contact due to the presence of ionic liquid.^{25,26} A schematic of the top gating method is shown in Fig. 1(a). By controlling this induced field due to capacitance, we have controlled the carrier concentration accumulation near the surface of graphene. The E_f of graphene can be controlled by the carrier concentration as discussed earlier.

The transfer of graphene from Cu to the substrate dopes graphene chemically and changes the E_f slightly. In order to find this new value, the charge neutrality point (CNP) is measured. It is the point where the resistance has a maximum value and the capacitance has a minimum value for the applied voltage. It is measured to be -0.6 V, and the relative E_f is 0.5 eV for simulations.²⁵

Reflection measurements for a PIR device was obtained by using a Fourier-transform infrared spectroscopy (FTIR) instrument integrated with a microscope. For the measurement, samples were illuminated with normal incidence. Measurements were done from 2.5 to $6.5 \,\mu\text{m}$ at different gate voltages using the top gating. The E_f of the graphene is changed from 0.5 eV to 0.8 eV for simulation in order to match the experimental curves obtained. These values are treated as fitting parameters as the I-V measurement similar to previous works.^{25,26,29}

The reflection simulation and experimental results are presented in Figs. 2(a) and 2(b), respectively. The PIR response is shifted toward shorter wavelengths as the E_f of graphene is increased, as shown in Fig. 2(a). As the gate voltage is increased from -0.6 V to 2.4 V, a blueshift is observed in the PIR-effect, shown in Fig. 2(b). The total shift of 211.7 nm was observed by changing the gate voltage of 3.0 V, presented in the inset of Fig. 2(b). The charge density in the graphene layer is increased by increasing the gate voltage from -0.6 V to 2.4 V. This will shift the resonance frequency of graphene, which is directly proportion to E_{f} . Therefore, the blueshift is observed by increasing E_f in this design. In order to quantitatively describe the change in the reflection intensity with the change in the E_f of graphene, the modulation depth in reflectance is defined as

$$M_{depth} = \frac{|(R - R_g)|}{R} \times 100.$$
(3)

Here, R is the reflection at -0.6 V and R_g is the reflection at 2.4 V. The modulation depth (M_{depth}) of 49% is realized at 4 μ m.

The E-field investigation of two strips is made for three different wavelengths, as shown in Fig. 3. Electric field magnitudes are presented at two resonance wavelengths (3.65 μ m and 4.42 μ m) in Figs. 3(a) and 3(c). Moreover, the E-field magnitude is shown at the PIR wavelength $(3.87 \,\mu\text{m})$ in Fig. 3(b). These figures show that both strips are excited separately at the resonance wavelengths and serve as the bright mode resonances. On the other hand, at 3.87 μ m, the PIR effect is produced by the simultaneous excitation of both strips.

The spectral contrast ratio (S_{con}) for PIR is used to evaluate the performance of devices in sensing or optoelectronic applications, and it is described as



FIG. 3. E-field magnitude at 0.8 eV: (a) E-field magnitude at 3.65 μ m, (b) Efield magnitude at 3.87 μ m, and (c) E-field magnitude at 4.42 μ m.

$$S_{con} = \frac{(R_{peak} - R_{dip})}{(R_{peak} + R_{dip})} \times 100, \tag{4}$$

where R_{peak} is the intensity of the reflection peak and R_{dip} is the intensity of the resonance dip. The S_{con} of our design is 66.6%. The PIR device is suitable for filtering and switching applications.

To summarize, PIR has been numerically investigated and experimentally realized using two strips on top of graphene. By changing the E_f of graphene, the PIR response was shifted. A large tuning range was demonstrated for the FTIR measurements of PIR structures by applying gate voltage. We were able to obtain a 211.7 nm shift in the reflection window and a modulation depth of 49% by applying gate voltage up to 3 V. These results of PIR can be used in many fields such as slow light applications and nonlinear optics.

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